

# Statistics for User Studies

A Practical Approach

# Accuracy vs. Precision

## **Accuracy**

is determined by  
**measurement errors**

needed:

**good study design**

verified by:

**thorough description  
of study setup**

## **Precision**

is determined by  
**measurement noise**

needed:

**enough data**

verified by:

**rigorous statistical  
analysis**

# Types of Data

- **Categorical / Nominal Data**

(alternatives in non-overlapping subsets,  $A=B$ ,  $A \neq B$ )

- Gender: male/female, Handedness: left/right

- **Ordinal Data**

(ranking/ordering  $A > B$ ,  $A < B$ ,  $A = B$ )

- Marks in school: 1, 2, 3, 4, 5, 6
- Type of education: school, high school, university

- **Interval Scale Data**

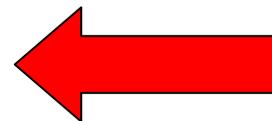
(zero point is arbitrary,  $A - B$ )

- tide
- temperature ( $^{\circ}\text{K}/^{\circ}\text{C}/^{\circ}\text{F}$ ),

- **Ratio Scale Data**

(fixed zero point  $A / B$ )

- weight
- time



**Try to get this!**

non-parametric

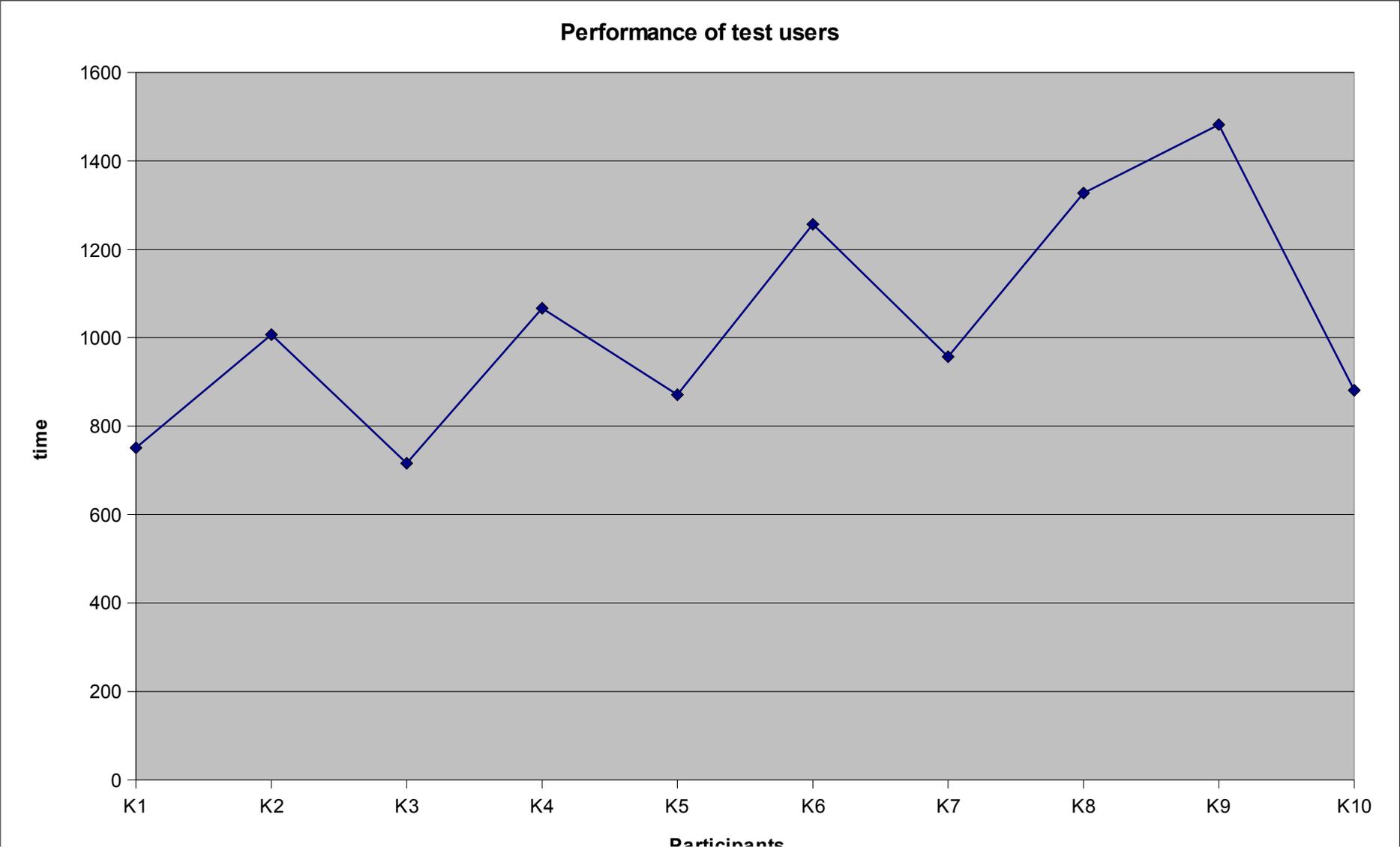
parametric

# Types of Variables

- Discrete Data
  - distinct and separate
  - can be counted
- Continuous Data
  - any value within a finite or infinite interval
  - always have an order

# Don't Do This

(in most cases)



# Frequency Tables

Data can be summarized in form of a frequency table

- well suited for discrete data
- continuous data have to be divided in groups

Example: days needed to answer my email

Data: 5 2 2 3 4 4 3 2 0 3 0 3 2 1 5 1 3 1 5 5 2 4 0 0 4 5 4 4 5 5

<i>Days</i>	<i>Frequency</i>	<i>Frequency (%)</i>
0	4	13%
1	3	10%
2	5	17%
3	5	17%
4	6	20%
5	7	23%

# Mean, Median, Mode (I)

## Mean

If  $x_1, x_2, \dots, x_n$  are the data in a sample, the mean is  $\frac{1}{n} \sum_{i=1}^n X_i$

## Median

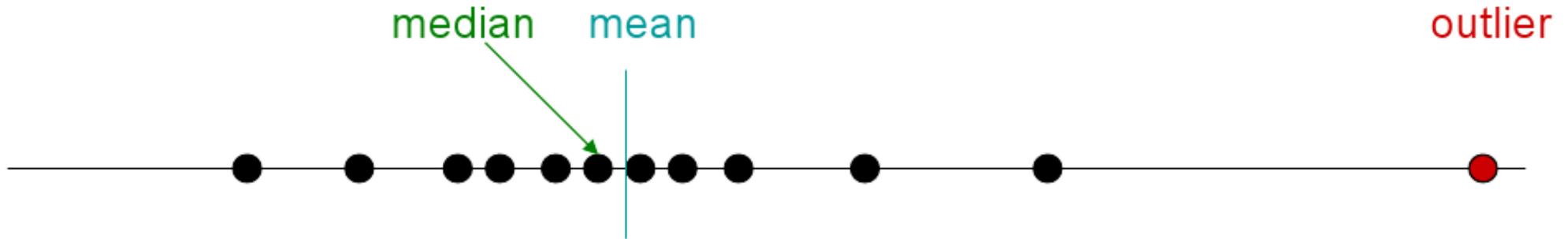
If  $x_1, x_2, \dots, x_n$  are the ordered data in a sample, the median is  $x_{(n+1)/2}$  if  $n$  is odd, and  $(x_{n/2} + x_{n/2+1}) / 2$  if  $n$  is even. It is the value halfway through the ordered data set.

## Mode

The mode is the value that occurs most often in a sample.  
There may be more than one mode in a sample.

# Mean, Median, Mode (II)

Median is less sensitive on outliers



Mode works on all types of data

Median works on ordinal, interval, ratio data

Mean works on interval or ratio data

# Likert Scales

## Examples:

PowerPoint presentations are the best way to teach. State your opinion.

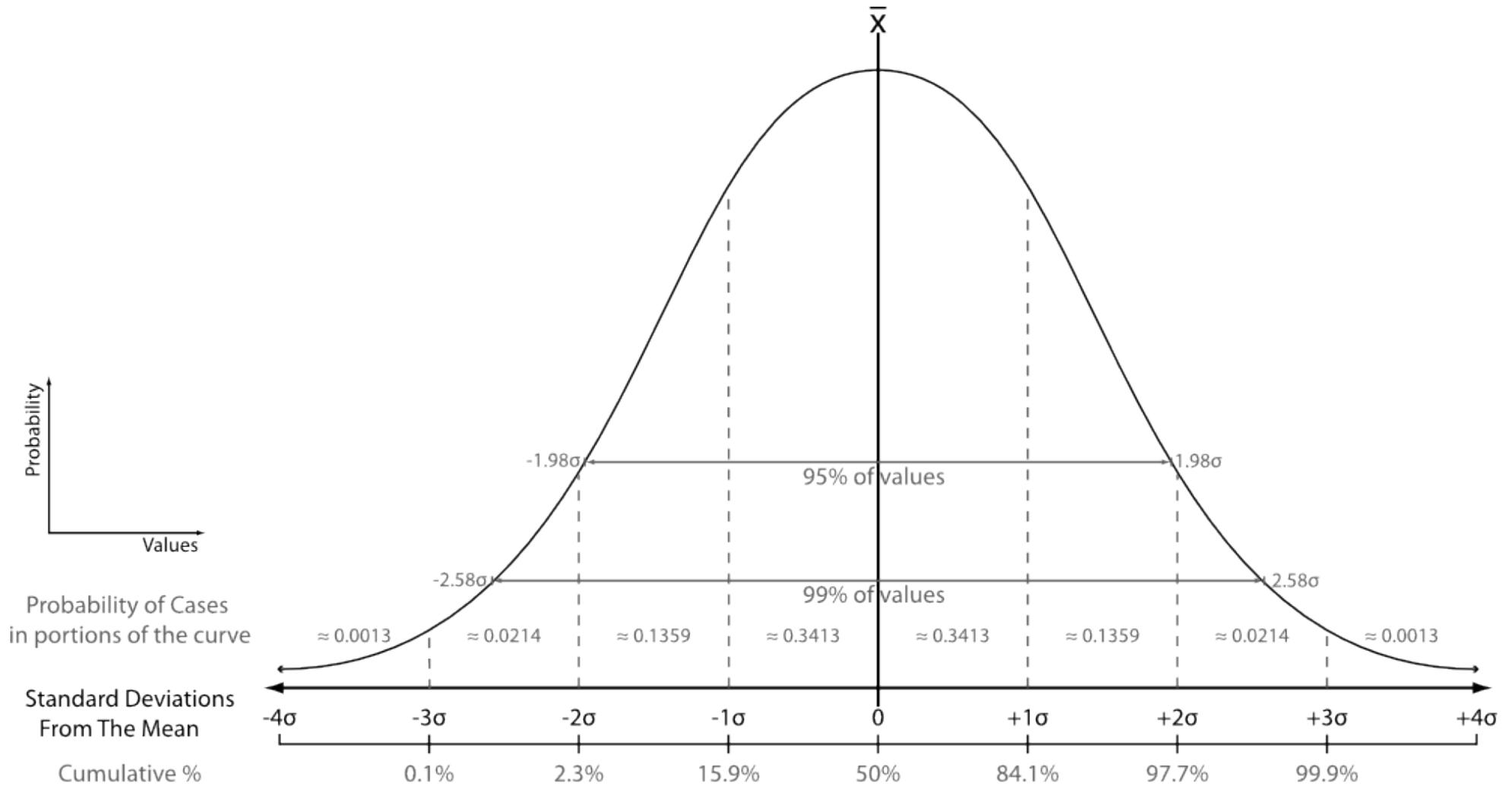
1. Strongly disagree
2. Disagree
3. Neither agree nor disagree
4. Agree
5. Strongly agree

This year I will buy a new computer.

- No       Uncertain       Yes

- ordinal data  
⇒ do not calculate mean!
- use sum-of-ranks
- you can force the user to make a commitment to one direction by offering an even number of choices.
- use 3 to 7 options

# Normal Distribution



Source: [http://en.wikipedia.org/wiki/Image:The\\_Normal\\_Distribution.svg](http://en.wikipedia.org/wiki/Image:The_Normal_Distribution.svg)

# Variance and Standard Deviation

## Variance

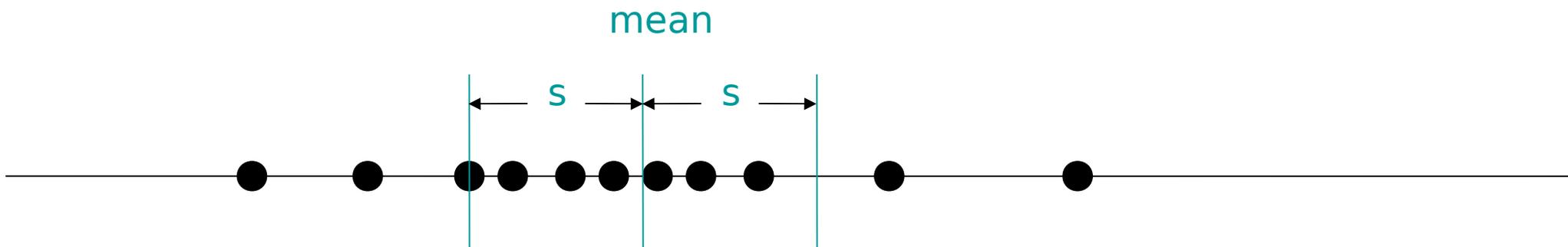
If  $x_1, x_2, \dots, x_n$  are the data in a sample with mean  $m$ , then the sample variance  $s^2$  is:  $s^2 = (\sum(x_i - m)^2) / n$

The larger the variance, the more scattered the observations on average.

*Caveat: many statistical software packages calculate the "bias-corrected sample variance", dividing by  $(n-1)$*

## Standard Deviation

The standard deviation  $s$  is the square root of the variance:  $s = \sqrt{\text{Var}(X)}$



# Quantile, Quartile, Percentile

## Quantile

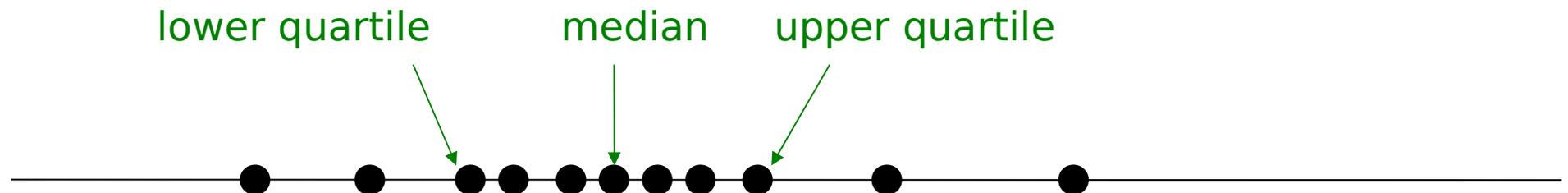
Quantiles are a set of 'cut points' that divide a sample of data into groups containing (as far as possible) equal numbers of observations.

## Quartile

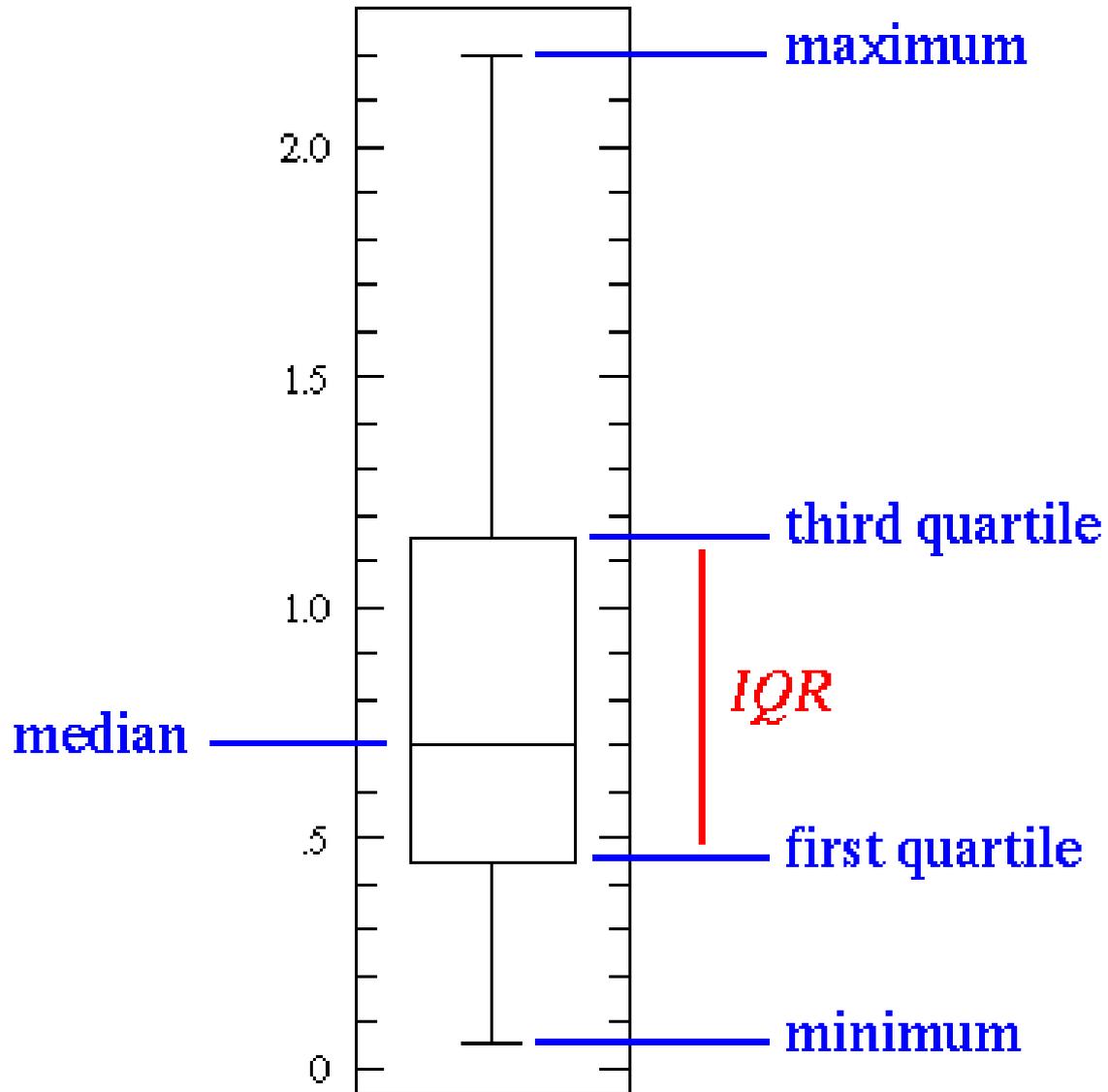
Quartiles are values that divide a sample of data into four groups containing (as far as possible) equal numbers of observations

## Percentile

Quartiles are values that divide a sample of data into hundred groups containing (as far as possible) equal numbers of observations



# Boxplot



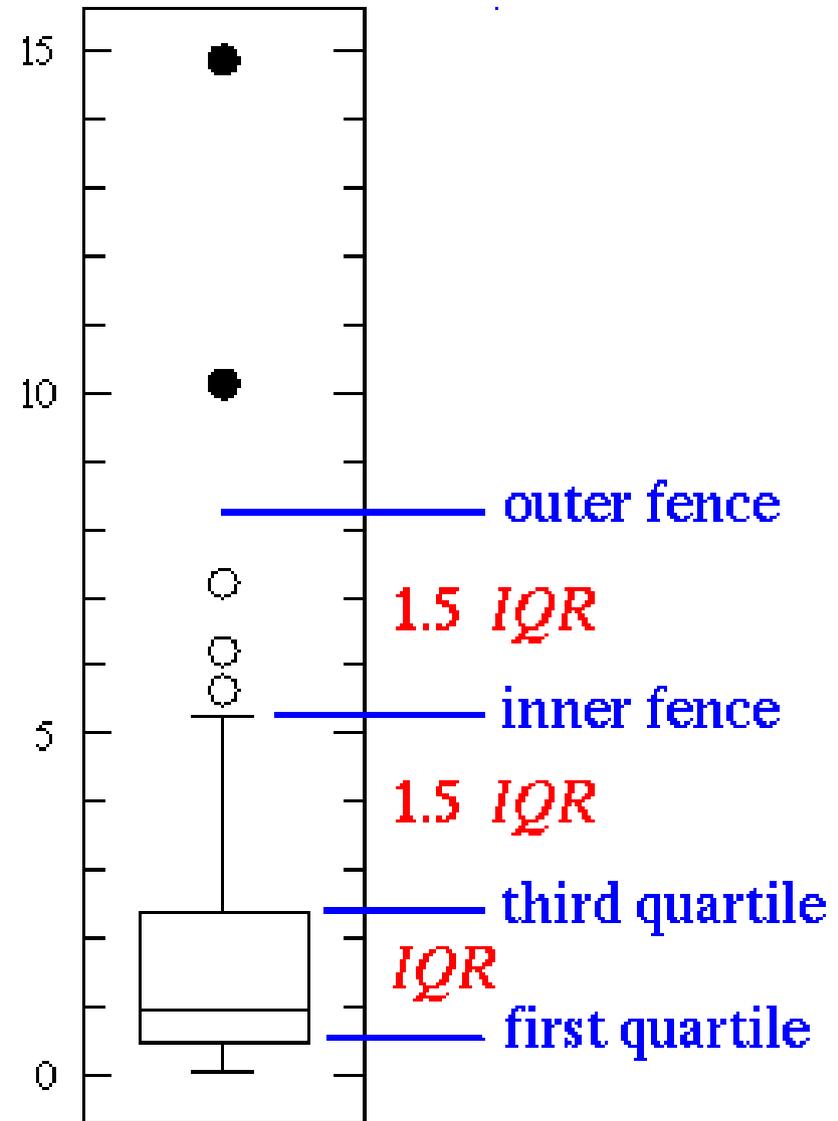
# Outliers

Try to avoid outliers

- Improve your test equipment
  - Eliminate sources of disturbances
  - Repeat parts of your experiment
- in case of disturbance

Outliers are not generally bad – they give you valuable information

With large data sets outliers can often not be avoided



# Some Excel Functions

## MEDIAN(Matrix)

- Matrix            Data row

## QUARTILE(Matrix; Quartil)

- Matrix            Data row
- Quartil            0 = min, 1=lower quartile, 2 = median, 3 = upper quartile, 4 = max.

## QUANTIL(Matrix; Alpha)

- Matrix            Data row
- Alpha            value form 0 to 1.

## Box Plots with Excel 2007

<http://blog.immeria.net/2007/01/box-plot-and-whisker-plots-in-excel.html>

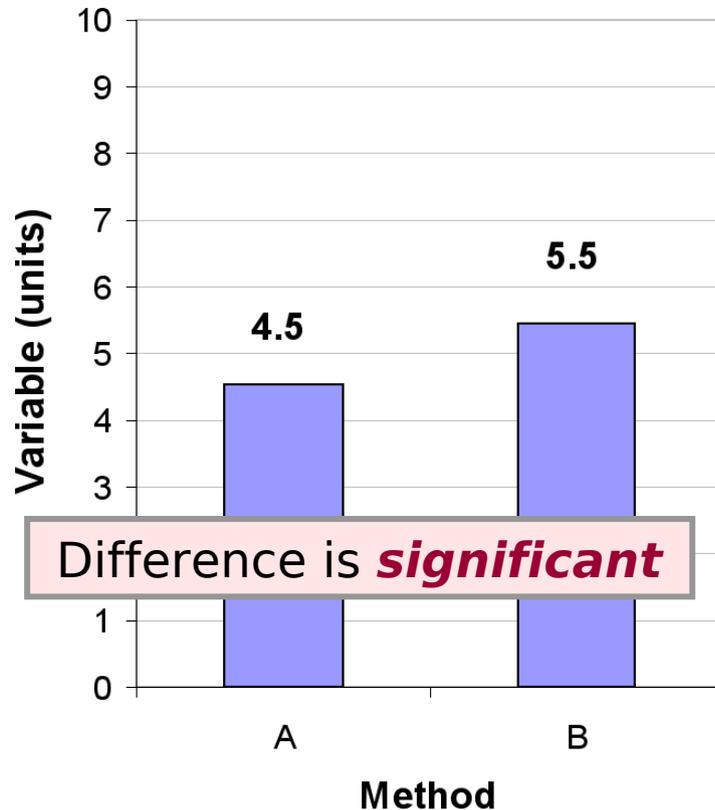
# Don't Do This (II)

“With version A the test users needed 25 seconds in average to complete the task, but with version B it took only 21 seconds. Thus, our user study showed that version B is the better way to solve the task.”

Is the difference significant?

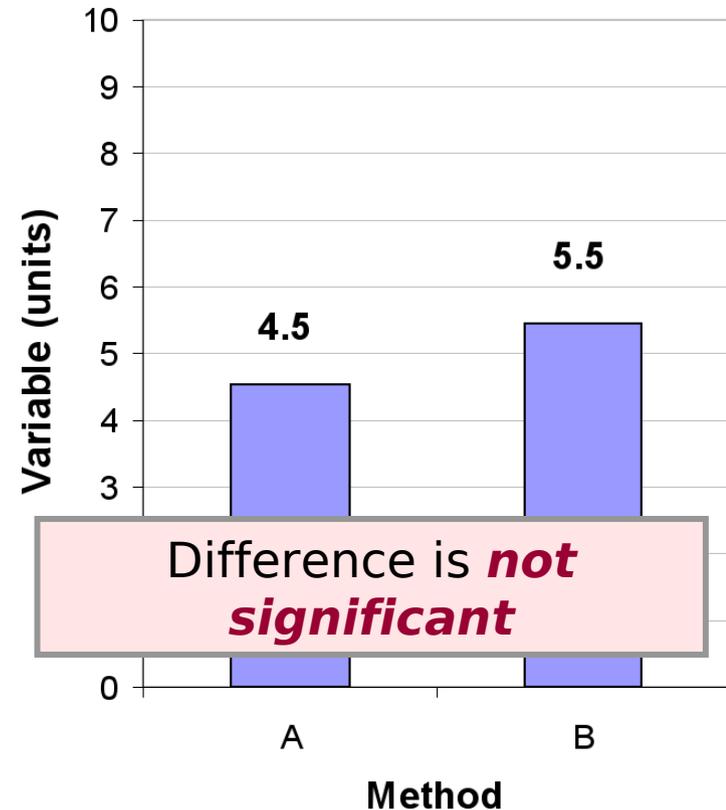
**What does 'significant' mean?**

# Example #1



“Significant” implies that in all likelihood the difference observed is due to the test conditions (Method A vs. Method B).

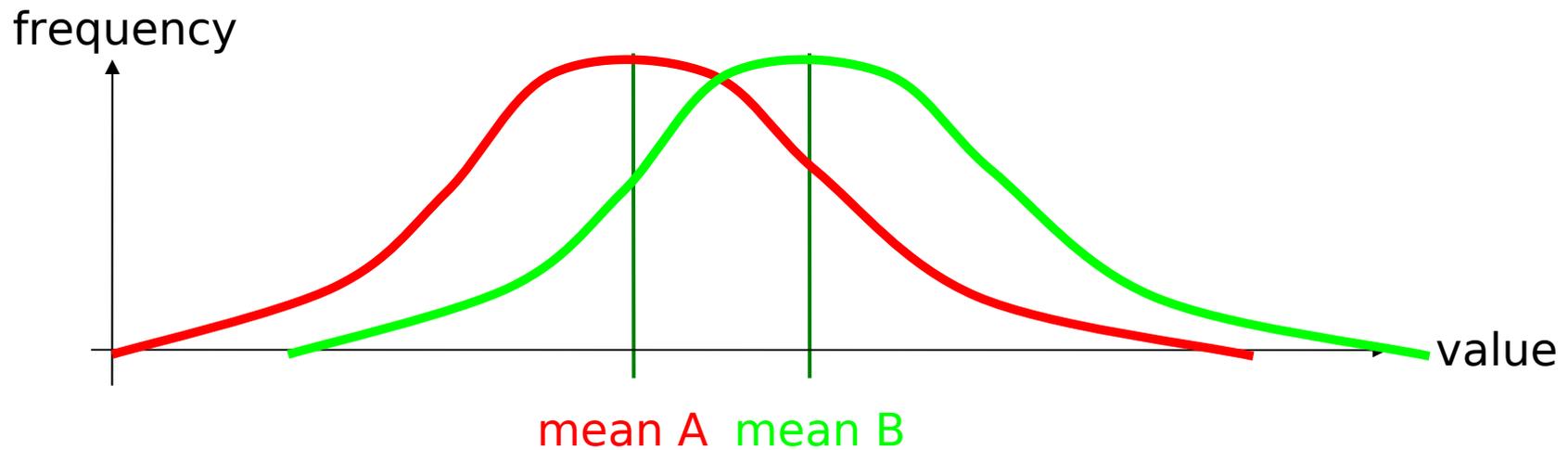
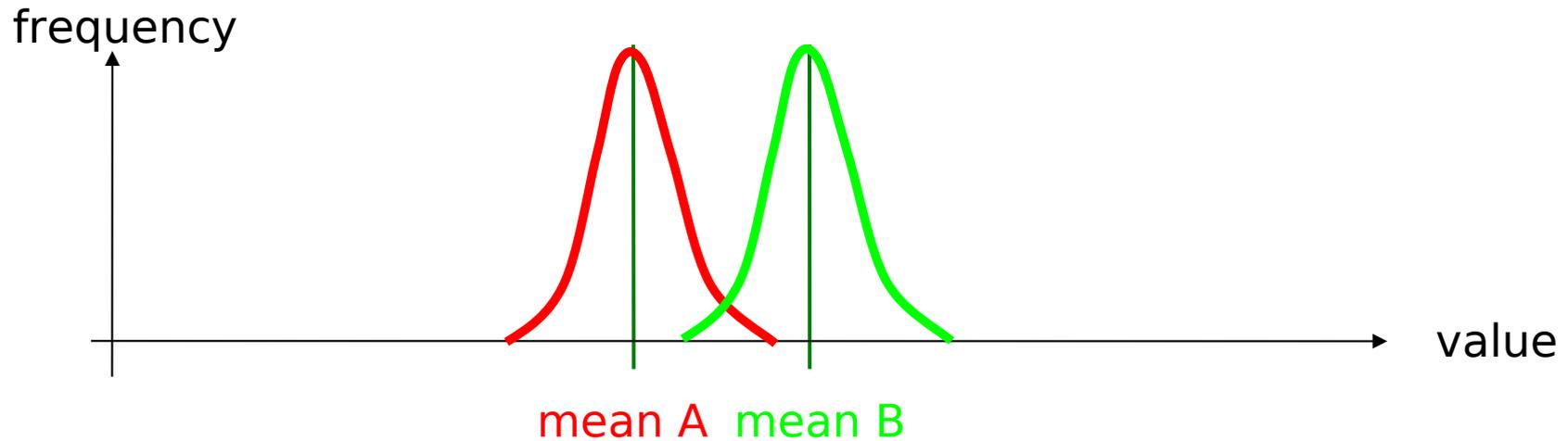
# Example #2



“Not significant” implies that the difference observed is likely due to chance.

# Comparing Values

Significant differences between measurements?



# Significance

In statistics, a result is called significant if it is unlikely to have occurred by chance.

It does not mean that the result is of practical significance!

A statistically significant speed difference of 0.1% between two text-entry methods may have little practical importance.

In the case of hypothesis testing the **significance level** is the probability that the null hypothesis ('no correlation') will be rejected in error although it is true.

Popular levels of significance are 5%, 1% and 0.1%

# Student's t-Test

The t statistic was introduced by William Sealy Gosset for cheaply monitoring the quality of beer brews. "Student" was his pen name. Gosset was a statistician for the Guinness brewery in Dublin.

The t-test is a test of the null hypothesis that the means of two **normally distributed** populations are equal. The t-test gives the probability that both populations have the same mean (and thus their differences are due to random noise).

A result of 0.05 from a t-test is a 5% chance for the same mean.

Different variants of the t-test are used for paired (each sample in population A has a counterpart in population B) and unpaired samples.

Examples:

**Paired:** speed of persons before and after treatment,

**Unpaired:** the reading speed of two different groups of people are compared

(mostly from wikipedia.org)

Student [William Sealy Gosset] (March 1908). "The probable error of a mean". *Biometrika* 6 (1): 1–25.

# Excel: t-Test

Real data from a user study

	A	B
K1	751	1097
K2	1007	971,5
K3	716	1121
K4	1066,5	1096,5
K5	871	932
K6	1256,5	926,5
K7	957	1111
K8	1327	1211,5
K9	1482	1062
K10	881	976
<b>Mean</b>	<b>1031,5</b>	<b>1050,5</b>

**T-test 0,8236863**

	A	B
K1	826,5	1382
K2	806	1066
K3	791	1276,5
K4	896,5	1352
K5	696	1191
K6	1121	1066
K7	891	1217
K8	1327	1412
K9	1277	1266,5
K10	656	1101
<b>Mean</b>	<b>928,8</b>	<b>1233</b>

**T-test 0,0020363**

Excel functions used:

```
=MITTELWERT(C4:C13)  
=TTEST(C4:C13;D4:D13;2;1)
```

(function names are localized)  
Menu: Tools>Data Analysis

TTEST(...) Parameters:

- Data row 1
- Data row 2
- Ends (1 or 2) (usually 2)
- Type (1=paired, 2=same variance, 3=different variance)

# T-Test Caveats

- can only be applied to two populations
- do not add significance levels from different tests

# Analysis of Variance (ANOVA)

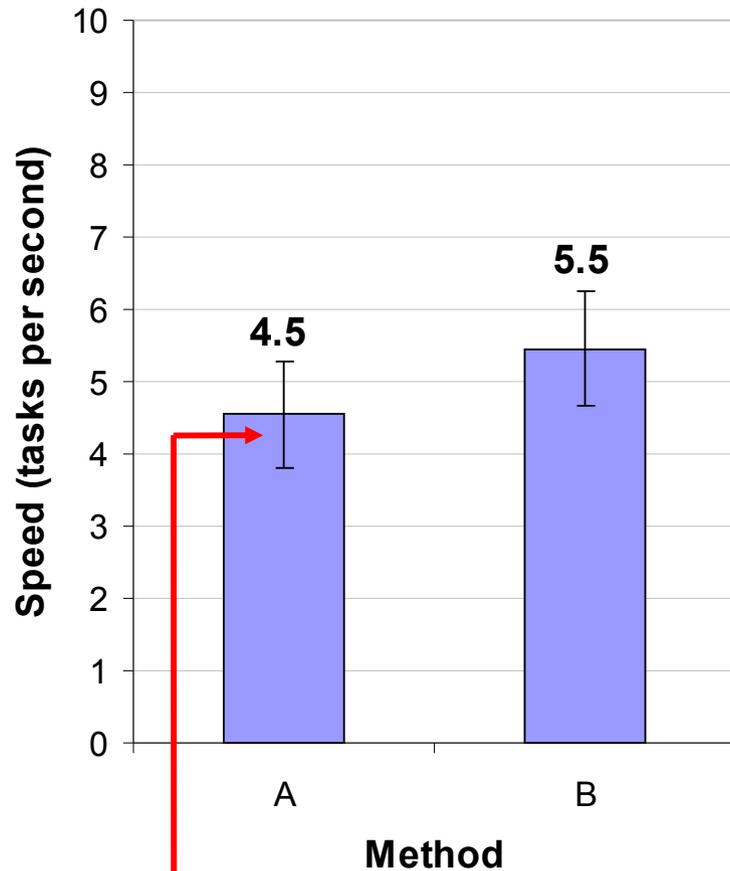
Determine if there is a significant difference between different series of measurements.

“Can the difference be explained by statistical noise?”

## General Concept:

- Calculate the variance within each measurement.
- Calculate the variance in relation to the mean of all series.
- If the variance within a measurement series is much smaller than the variance in relation to the overall mean → significant!

# Example #1 - Details



Error bars show  
 $\pm 1$  standard  
deviation

Example #1		
Participant	Method	
	A	B
1	5,3	5,7
2	3,6	4,6
3	5,2	5,1
4	3,3	4,5
5	4,6	6,0
6	4,1	7,0
7	4,0	6,0
8	5,0	4,6
9	5,2	5,5
10	5,1	5,6
<i>Mean</i>	4,5	5,5
<i>SD</i>	0,73	0,78

# Example #1 - Anova

ANOVA Table for Speed

	DF	Sum of Squares	Mean Square	F-Value	P-Value	Lambda	Power
Subject	9	5.839	.649				
Method	1	4.161	4.161	8.443	.0174	8.443	.741
Method * Subject	9	4.435	.493				

Probability that the difference in the means is due to chance

Reported as...

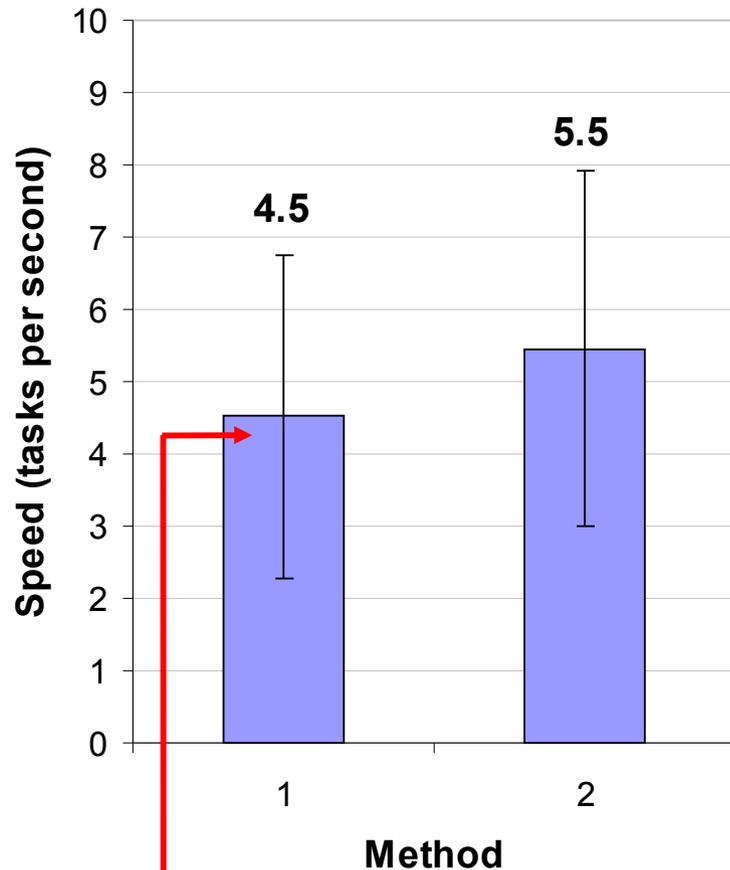
$$F_{1,9} = 8.443, p < .05$$

Thresholds for "p"

- .05
- .01
- .005
- .001
- .0005
- .0001

$$F = \frac{\text{explained variance}}{\text{unexplained variance}}$$

# Example #2 - Details



Error bars show  $\pm 1$  standard deviation

Example #1		
Participant	Method	
	A	B
1	5,3	5,7
2	3,6	4,6
3	5,2	5,1
4	3,3	4,5
5	4,6	6,0
6	4,1	7,0
7	4,0	6,0
8	5,0	4,6
9	5,2	5,5
10	5,1	5,6
<i>Mean</i>	4,5	5,5
<i>SD</i>	0,73	0,78

# Example #2 – Anova

ANOVA Table for Speed

	DF	Sum of Squares	Mean Square	F-Value	P-Value	Lambda	Power
Subject	9	37.017	4.113				
Method	1	4.376	4.376	.634	.4462	.634	.107
Method * Subject	9	62.079	6.898				

Probability that the difference in the means is due to chance

Reported as...

$$F_{1,9} = 0.634, ns$$

Note: For non-significant effects, use "ns" if  $F < 1.0$ , or " $p > .05$ " if  $F > 1.0$ .

# Excel: ANOVA

Anova: Single Factor  
**Which Bowler is Best?**  
 SUMMARY

Tools Menu  
 → Data Analysis  
 → One-Way  
 ANOVA

Groups	Count	Sum	Average	Variance
Pat	6	922	153.6667	92.26667
Mark	6	1070	178.3333	116.6667
Sheri	6	937	156.1667	54.96667

ANOVA

Source of Variation	SS	df	MS	F	P-value	F crit
Between Groups	2212.111	2	1106.056	<b>12.57358</b>	0.000621	<b>3.682317</b>
Within Groups	1319.5	15	87.96667			
Total	3531.611	17				

Source: <http://www.isixsigma.com/library/content/c021111a.asp>

ANOVA test online: <http://www.physics.csbsju.edu/stats/anova.html>

Java API for ANOVA: <http://www.yorku.ca/mack/RN-Anova.html>

# This Lecture is not Enough!

We strongly recommend to teach yourself.  
There is plenty of material on the WWW.

## Further Literature

Andy Field & Graham Hole: How to design and report experiments, Sage

- Jürgen Bortz: Statistik für Sozialwissenschaftler, Springer
- Christel Weiß: Basiswissen Medizinische Statistik, Springer
- Lothar Sachs, Jürgen Hedderich: Angewandte Statistik, Springer
- various books by Edward R. Tufte