

# 7. Hierarchies & Trees

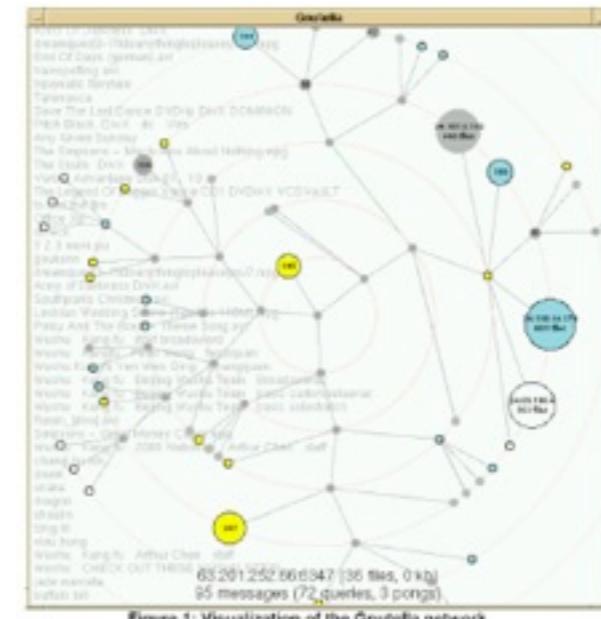
## Visualizing topological relations

Vorlesung „Informationsvisualisierung“  
Prof. Dr. Andreas Butz, WS 2012/13  
Konzept und Basis für Folien: Thorsten Büring

# Outline

- Hierarchical data and tree representations
- 2D Node-link diagrams
  - Hyperbolic Tree Browser
  - SpaceTree
  - Cheops
  - Degree of interest tree
  - 3D Node-link diagrams
- Enclosure
  - Treemap
  - Ordererd Treemaps
  - Various examples
  - Voronoi treemap
  - 3D Treemaps
- Circular visualizations
- Space-filling node-link diagram

# Hierarchical Data

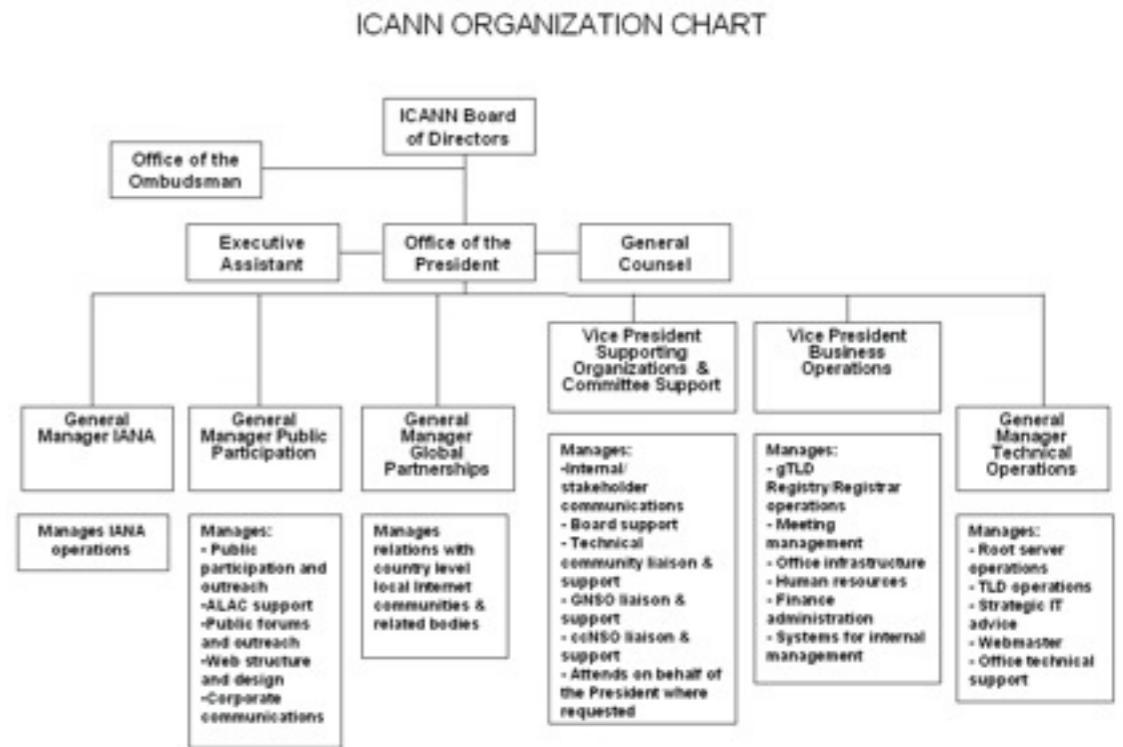


Yee et al. 2001  
see previous  
lecture...

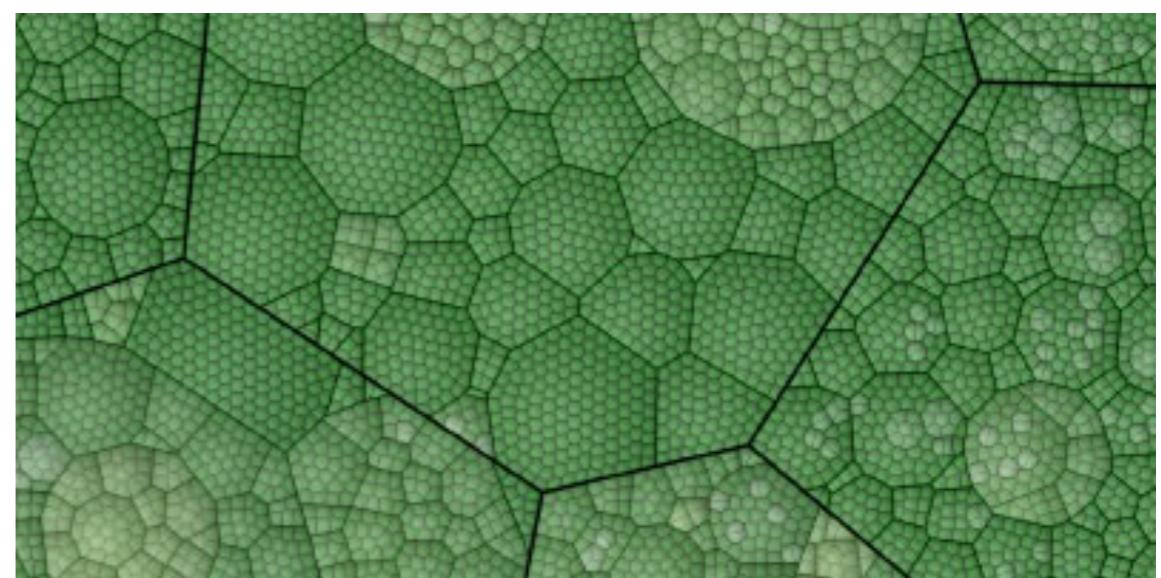
- Hierarchies are usually represented as tree visual structures
  - Trees tend to be easier to lay out and interpret than networks (e.g. no cycles)
  - But: as shown in the example, networks may in some cases be visualized as a tree

# Tree Representations

- Two kinds of representations
- Node-link diagram (see previous lecture): represent connections as edges between vertices (data cases)
- Enclosure: space-filling approaches by visually nesting the hierarchy

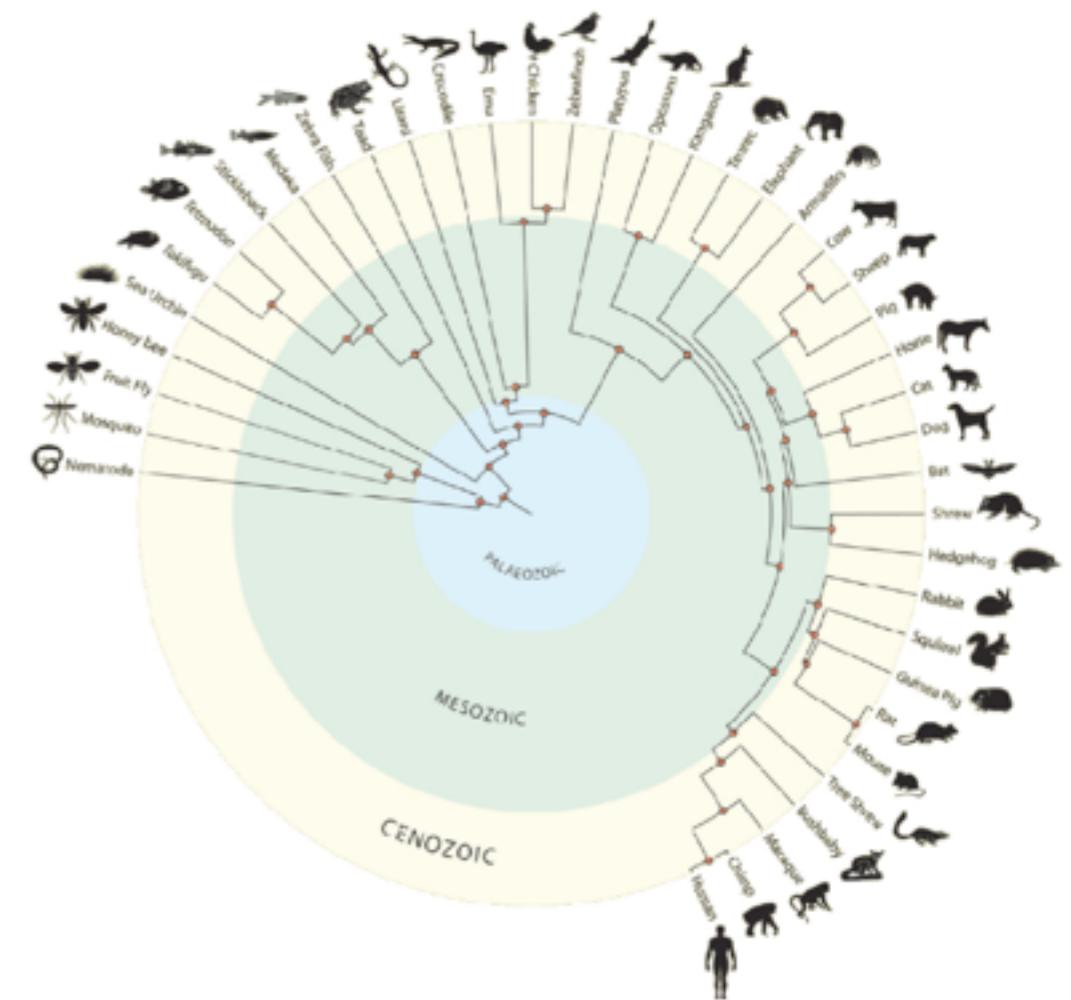
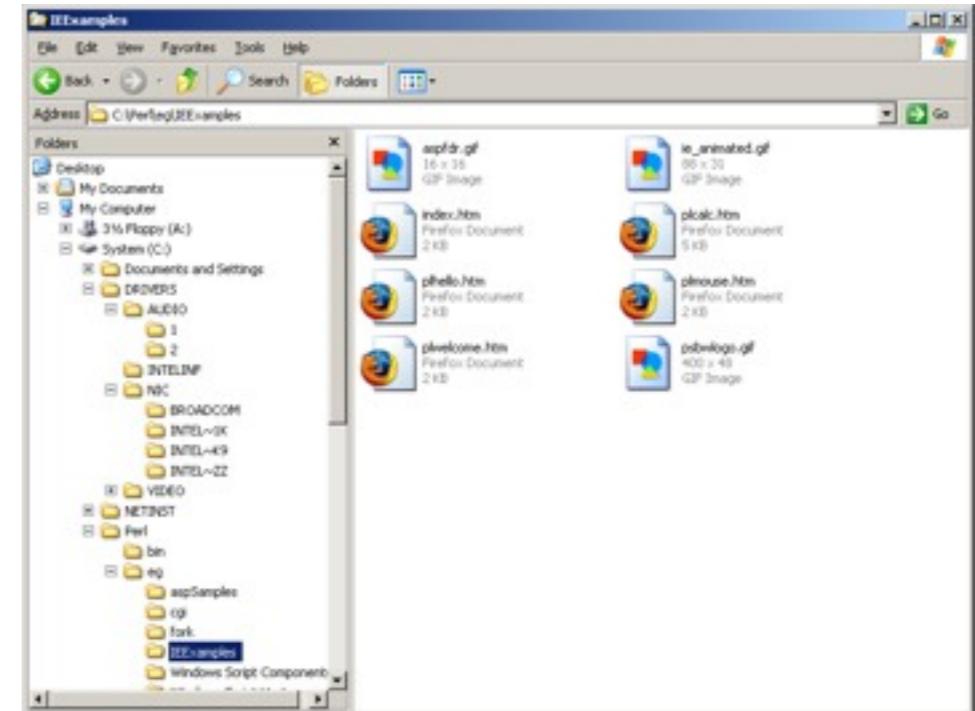


<http://www.icann.org>



# Node-Link Diagram

- Most conventional layout
    - Tree-depth is mapped to an ordinal Y-axis
    - X-axis is nominal – mainly used to separate siblings
  - Can also be turned around
  - Circular layout – root in the center with levels growing outward



# Node-Link Diagram

- Unlike space-filling methods, node-link diagrams provide an effective overview of the topology of a tree
- Problems:
  - Large trees require an extreme aspect ratio
    - Example: branching factor of 2
    - Tree gets wider approximately proportionally  $2^n$  ( $n = \text{level}$ ) ...
    - ... and taller only proportionally to  $n$
    - Large trees become to resemble a straight line
  - Trees usually contain considerable empty space (about 50%)
  - InfoVis approaches to address these problems
    - Interaction
    - Distortion

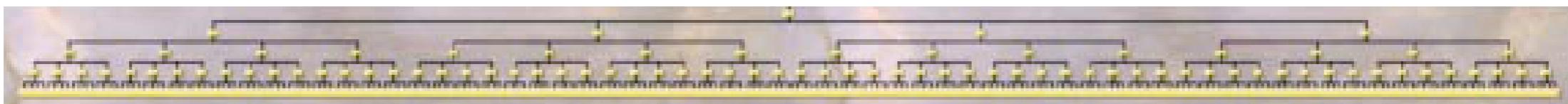


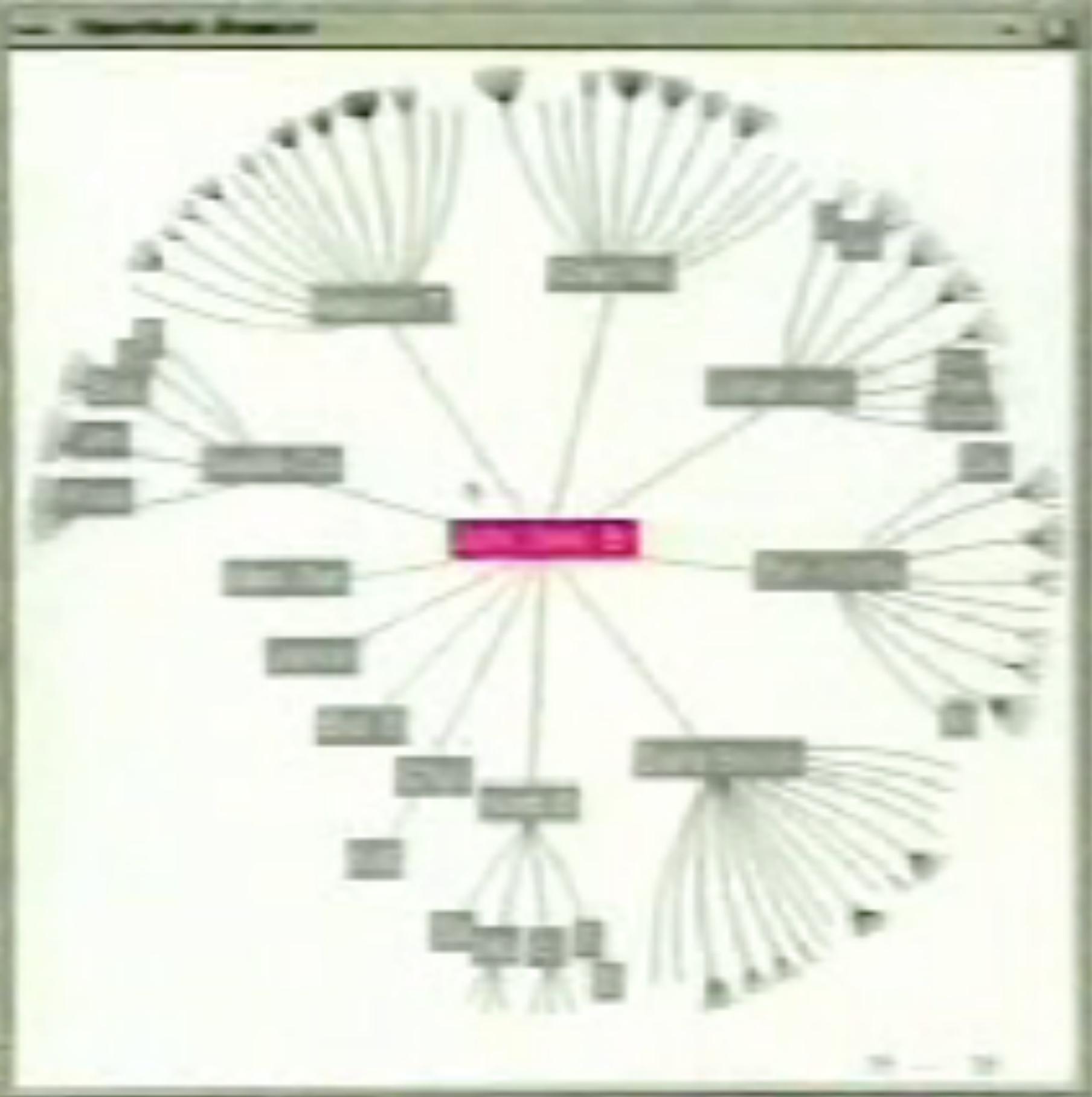
Image from: <http://davenation.com/doitree/doitree-avi-2002.htm>

# Hyperbolic Tree Browser

Inspiration:  
Circle Limit IV  
M.C. Escher



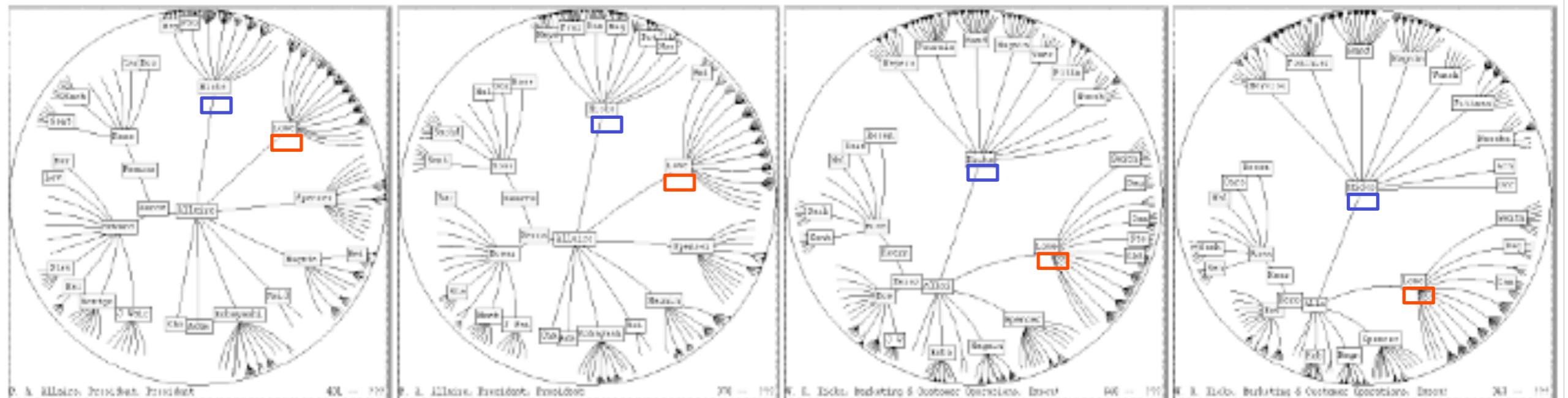
- Lamping et al. 1995
- Comparable to fisheye distortion
  - Nodes in the center are displayed at higher granularity
  - Neighboring nodes are displayed in diminishing size
- Maximum number of nodes displayed in a 600 x 600 pixel window
  - Standard 2D hierarchy browser: typically 100 nodes with 3 characters text labels
  - Hyperbolic browser: can display 1000 nodes with 50 nearest the focus can show from 3 to dozens of characters text labels
- Approach exploits hyperbolic geometry
  - Lay out hierarchy on hyperbolic plane and map plane onto a circular display region
  - Property of hyperbolic plane: circumference of a circle grows exponentially with its radius
  - Hierarchies tend to expand exponentially with depth
  - Elegant match!



# Hyperbolic Tree Browser

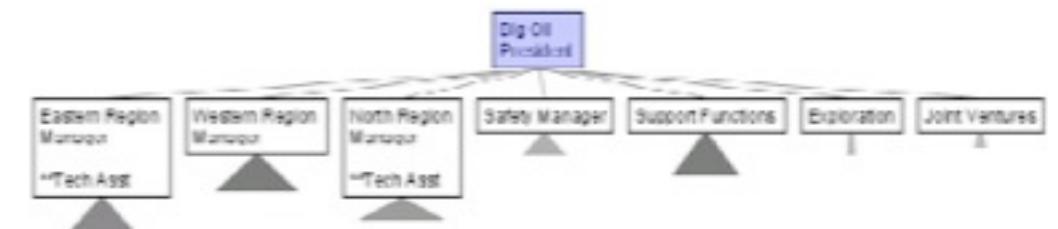
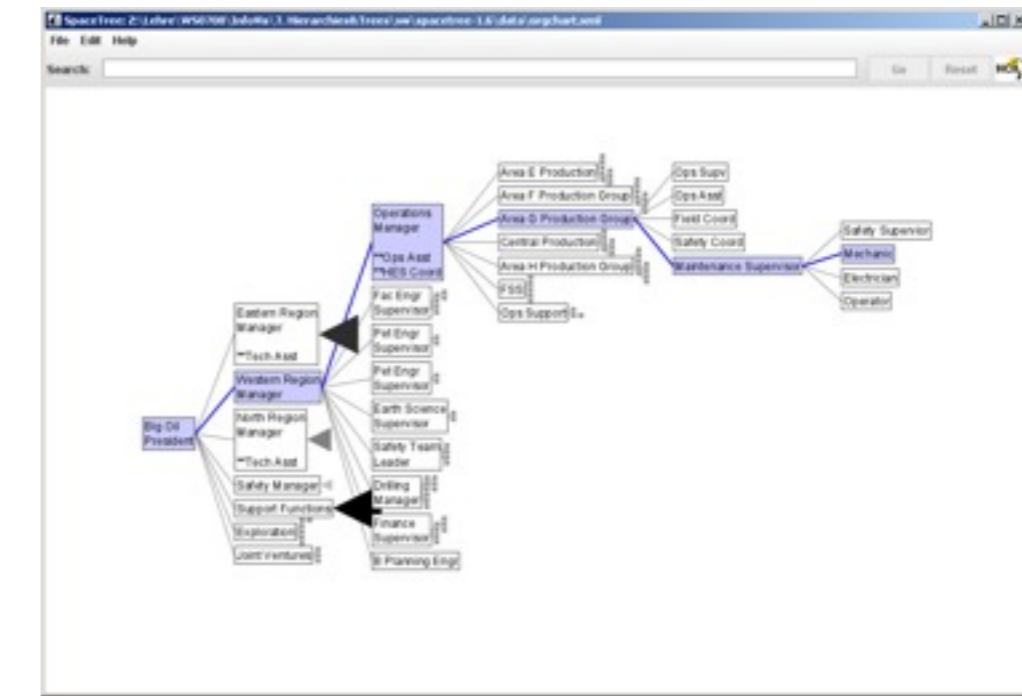
- Navigation: users select nodes to become the new center node (animated transitions)
- Potential problem with orientation:
  - nodes rotate during pure translation, e.g. node “Lowe” moves from top right to bottom right
  - Not suitable to present data such as organizational charts
- Small-scale user test (4 subjects, within-subjects design, IV: type of browser, DV: number of actions, time, preference)
  - No significant performance advantage over a 2D hierarchy browser with horizontal tree layout
  - Participants preferred the hyperbolic tree browser - provided “weaker sense of directionality of links”, but helped to “get(ting) a sense of the overall tree structure”

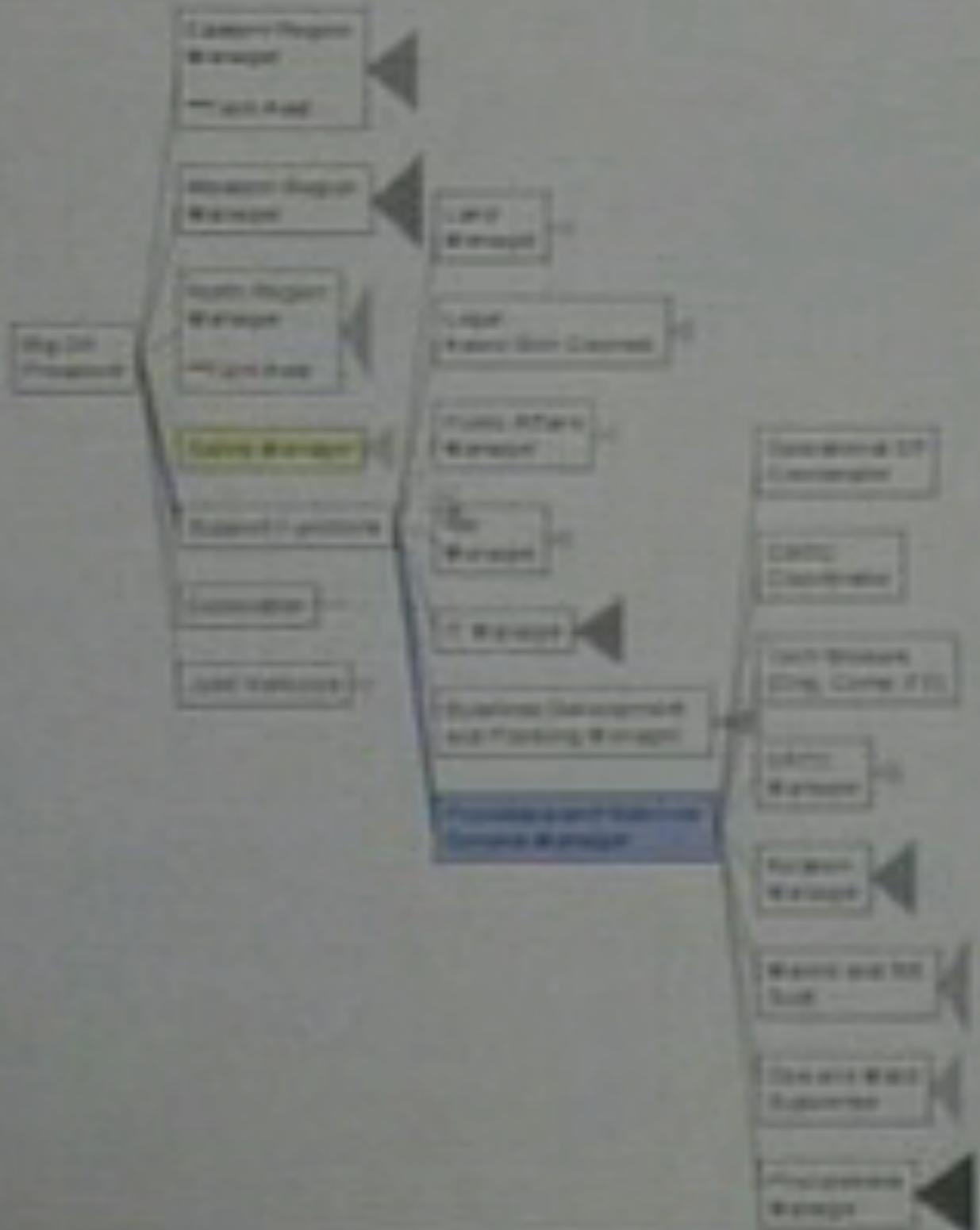
Lamping et al. 1995



# SpaceTree

- Plaisant et al. 2002
- Mechanisms to facilitate large tree exploration / navigation
  - Dynamic rescaling of branches to fit the screen
    - De-composed animated transitions
  - Optimized camera movement
  - Preview icons summarizing branches collapsed (see top-down order)
    - Shading of triangle is proportional to the total number of nodes in the subtree
    - Height of triangle represents depth of subtree
    - Base of triangle proportional to average width (number of items / depth)
  - Search and filter functionality
- Video



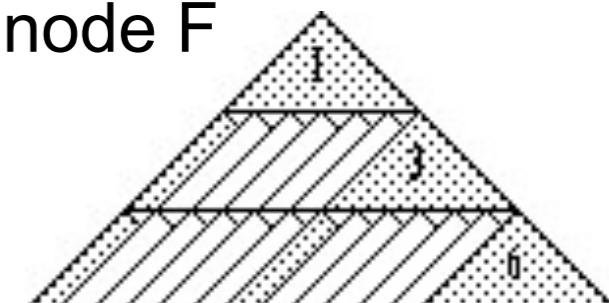
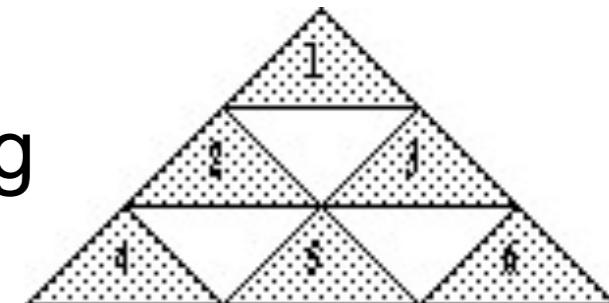
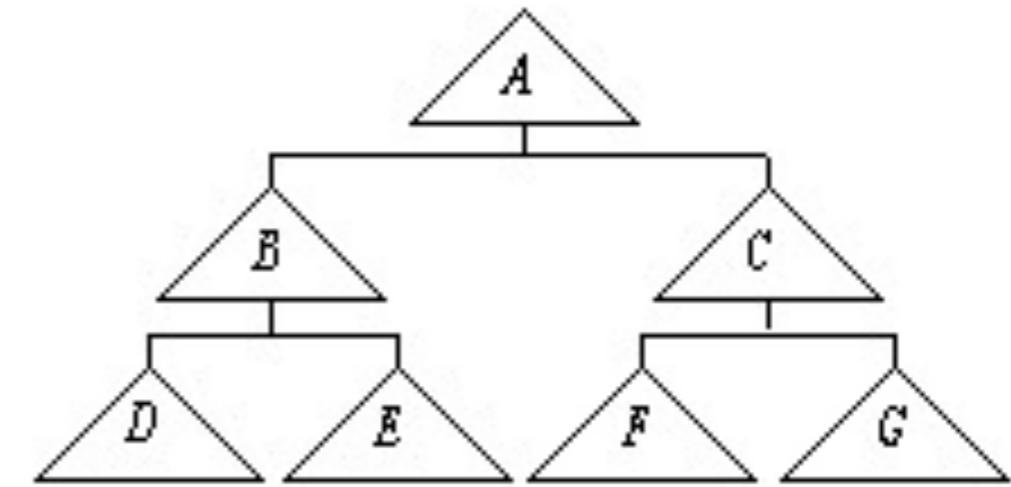


# SpaceTree

- Experiment comparing 3 tree-browsing interfaces
  - Microsoft Explorer
  - Hyperbolic tree browser
  - SpaceTree
- Counterbalanced repeated-measures within-subject design
- 18 participants
- Tree with 7000 nodes
- Three task types
  - Node searches
  - Search of previously visited nodes
  - Answering topology questions
- Results
  - Hardly significant performance differences between the interfaces
  - Users found MS Explorer significantly less attractive than the other two interfaces

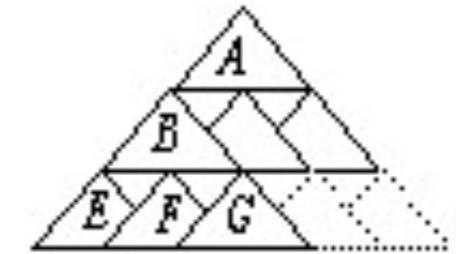
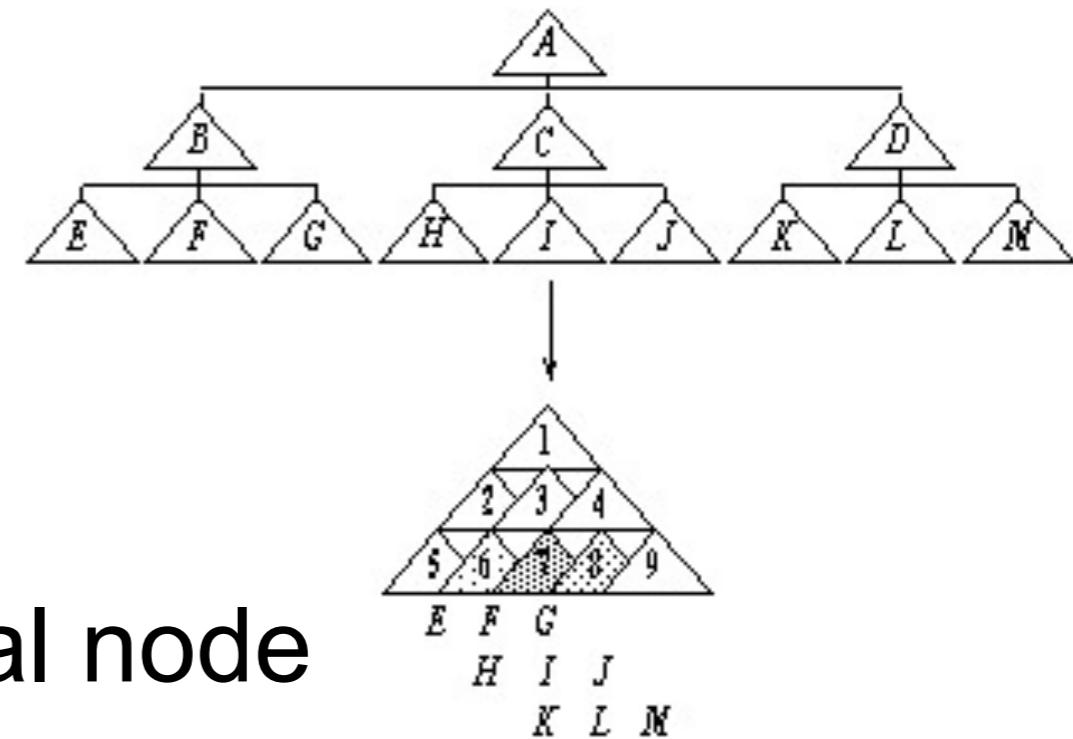
# Cheops

- Beaudoin et al. 1996
- Exploring and navigating large graphs
  - Maintain context
  - Provide easy access to details
- Cheops provides effective compression by reusing visual components based on interaction
- Compress the hierarchy by tessellation of triangles
  - In the example triangle 5 could represent either node E or node F
  - If triangle 2 is selected, triangle 5 will become node E ...
  - Overlapping triangles to indicate larger hierarchy
  - The example shows an expansion by adding 5 children per parent
- But: users cannot compare topologically remote parts of a structure



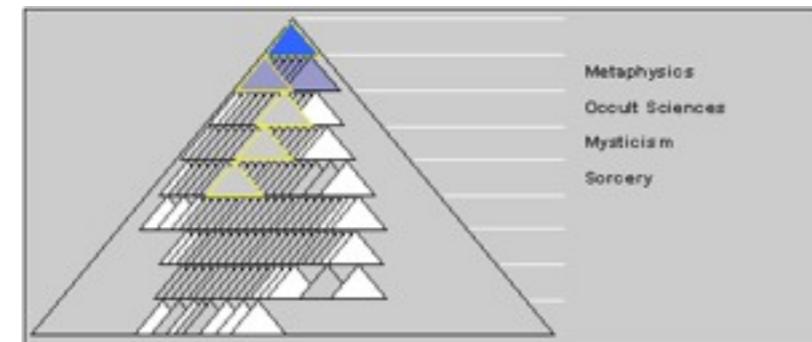
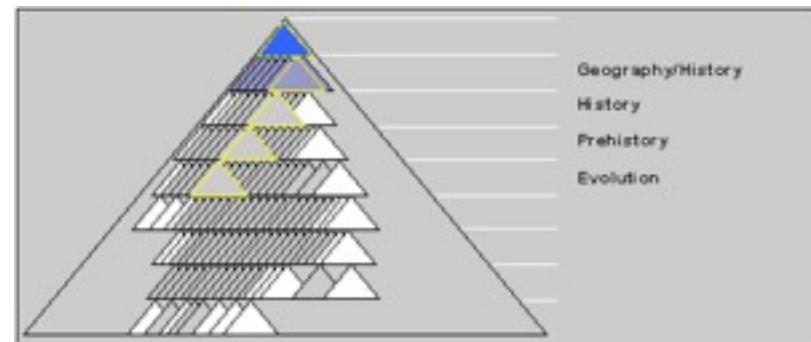
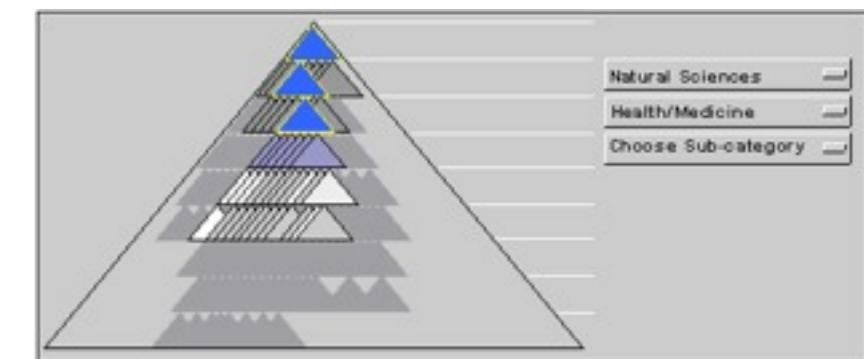
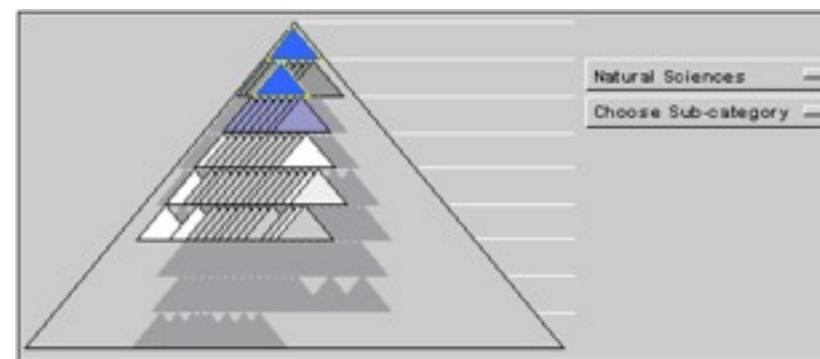
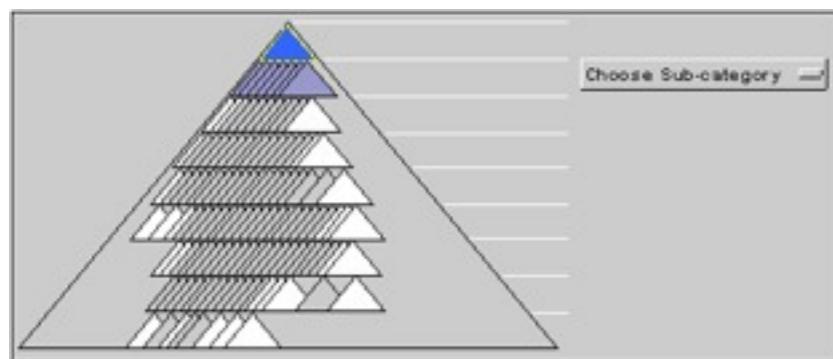
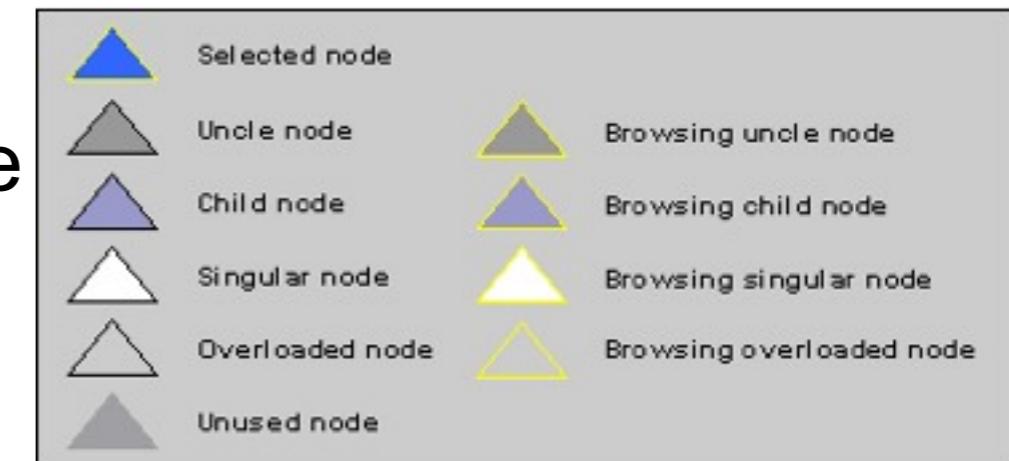
# Cheops

- Another example
- Three triangles in the last level represent more than one logical node
- If a parent node (e.g. B) is selected the visual components become unambiguous
- Selection of a node implies previous selection of all its parent nodes
- Nodes are represented as paths of visual objects going down from the root – not isolated triangles



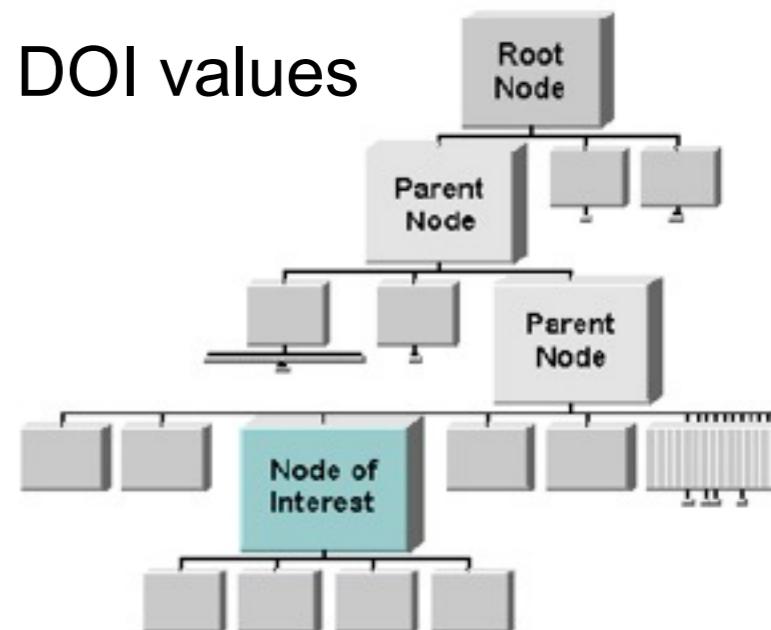
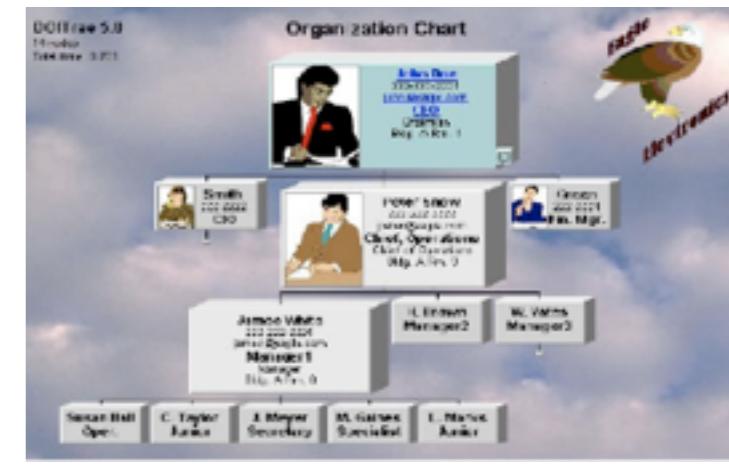
# Cheops

- Visual cues and terminology to aid interpretation of the compressed visualization
- Selection: deployment of branches
- Pre-selection: direct access to any node



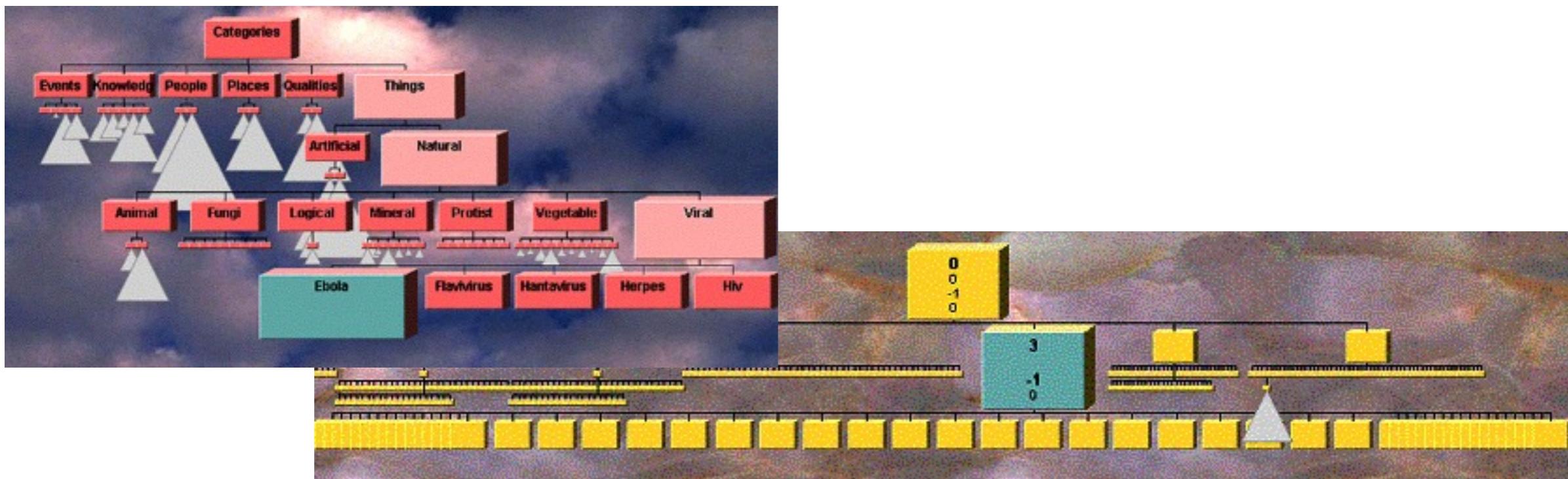
# Degree of Interest Tree

- Nation et al. 2002
- For interactive display of hierarchies within a web browser
- Based on Furnas Degree-of-interest function
  - Each node is assigned a value
  - Degree-of-interest value is determined by a function of a node's distance from the root of the tree and its distance from the focus of interest
  - Topic of later lecture on focus+context presentation techniques!
- DOI Tree
  - Upon selection: focused node is allocated most space
  - Remaining space is allocated to nodes based on their DOI values
  - Nodes with more space present more details



# Degree of Interest Tree

- Animated transitions
- Reset the tree layout by clicking on the root node
- Tree does not fit the screen in the Y-dimension
  - Prune parts of the tree below a given DOI threshold
  - Pruned branch is represented by a symbol
- Tree does not fit the screen in the X-dimension – visually compress peripheral nodes



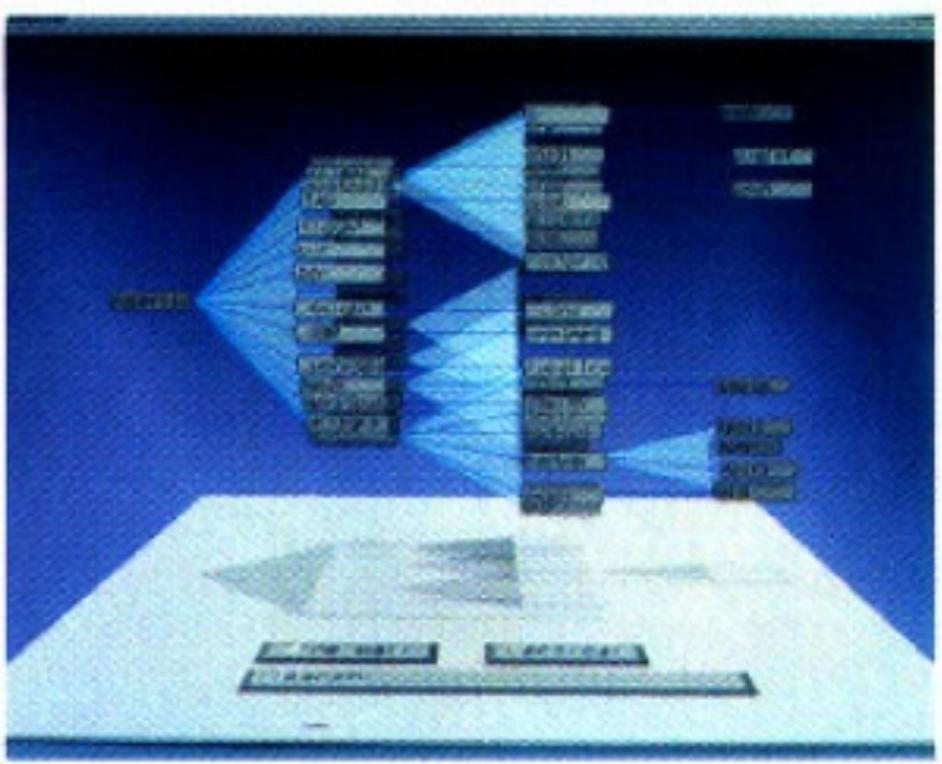
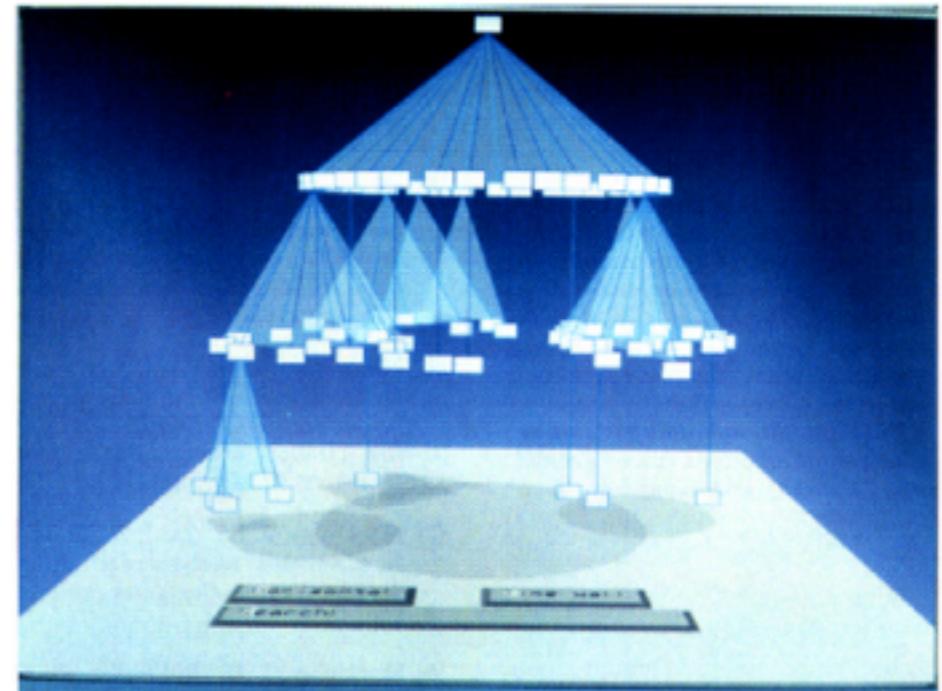
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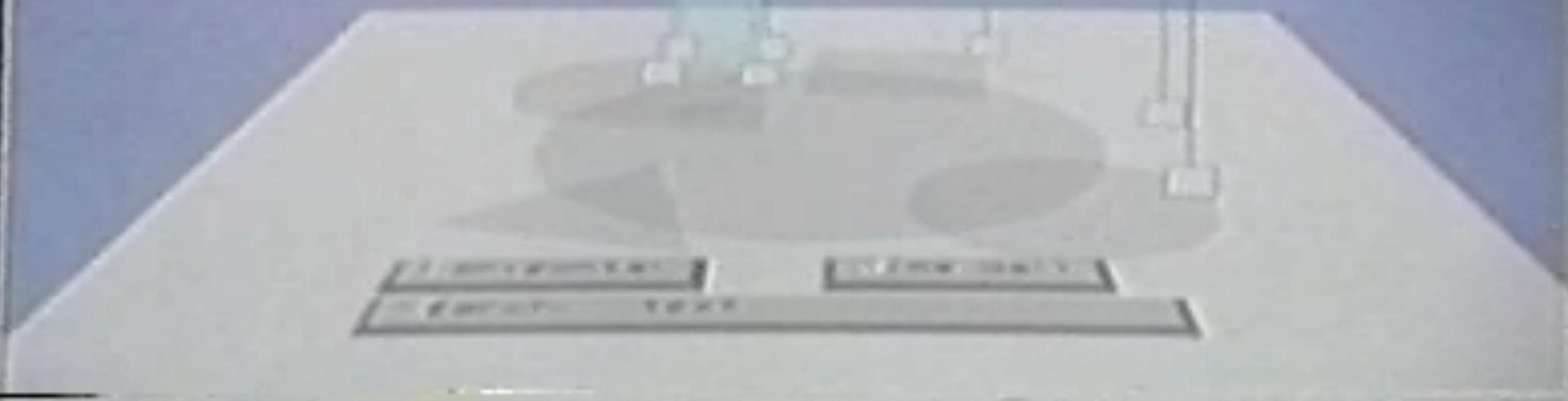
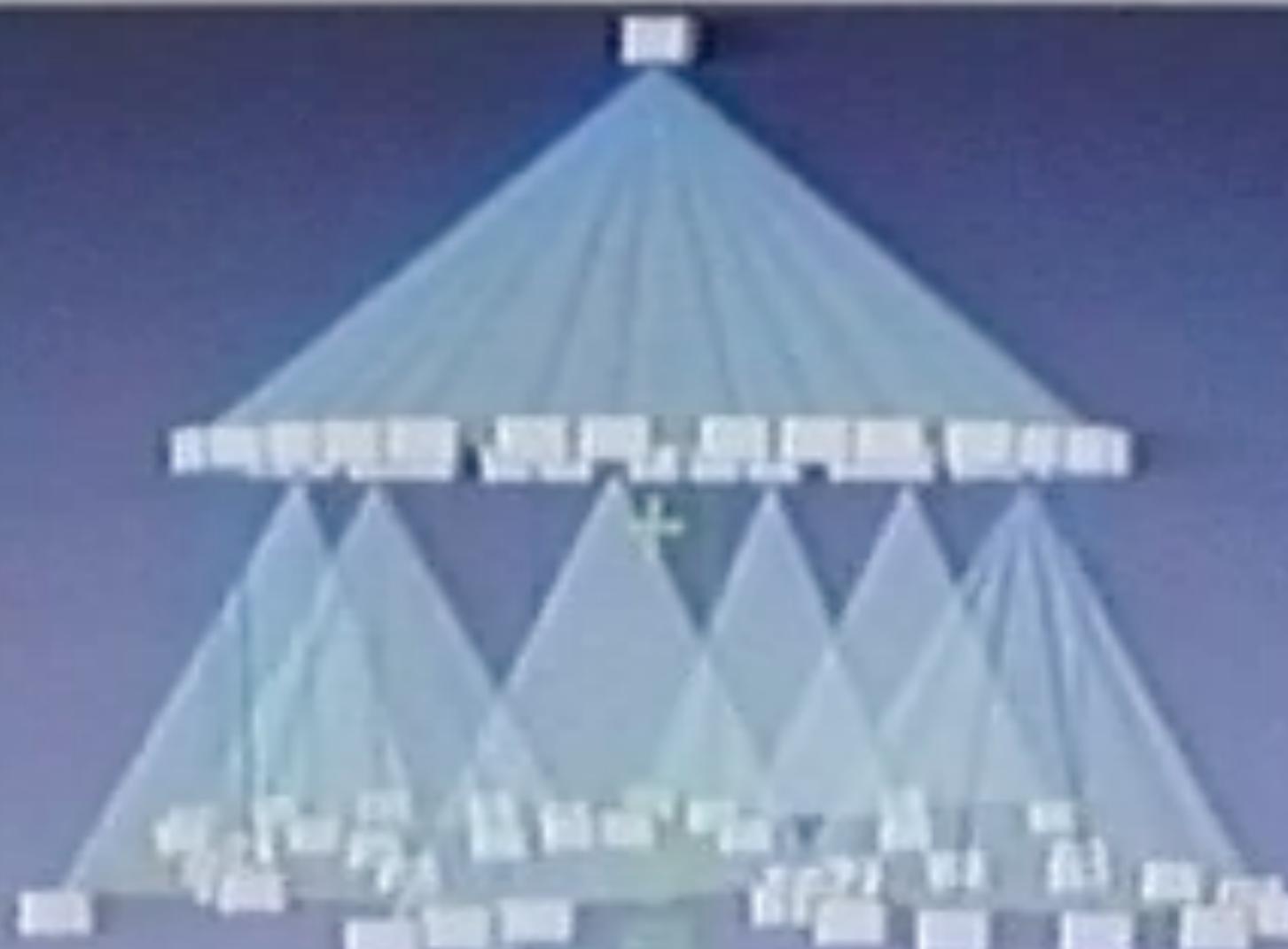
# 3D Approaches

- Why not use an additional dimension to visualize nodes that would otherwise be pruned / collapsed?
  - Cone Tree
  - H3Viewer
- HCI research produced mixed results about the usability of 3D interfaces
- Ongoing research question: do 2D interfaces better exploit the abilities of the human perceptual system?
  - Utilize spatial memory?
  - Controlling 3D navigation with 2D input devices?
- 3D node-link approaches have been mainly researched in the 90s

# Cone Tree

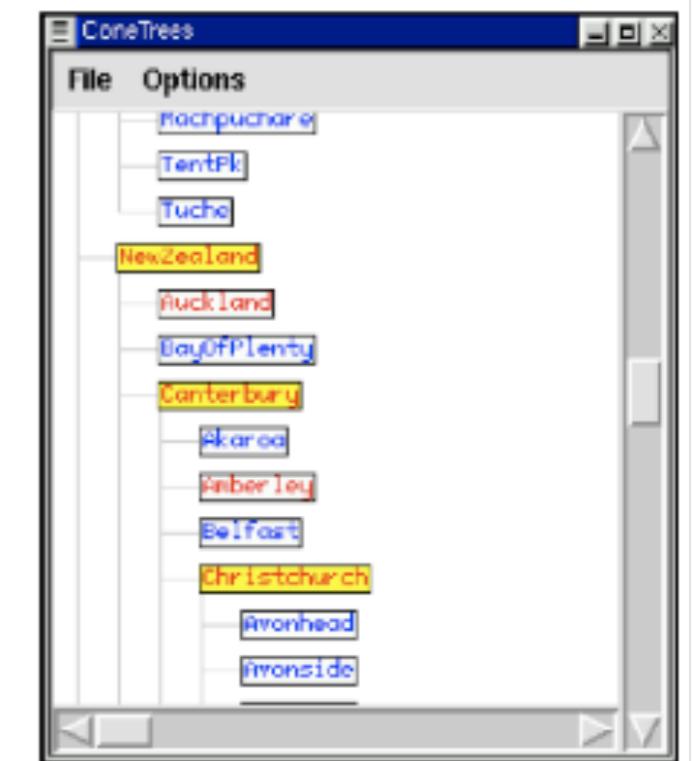
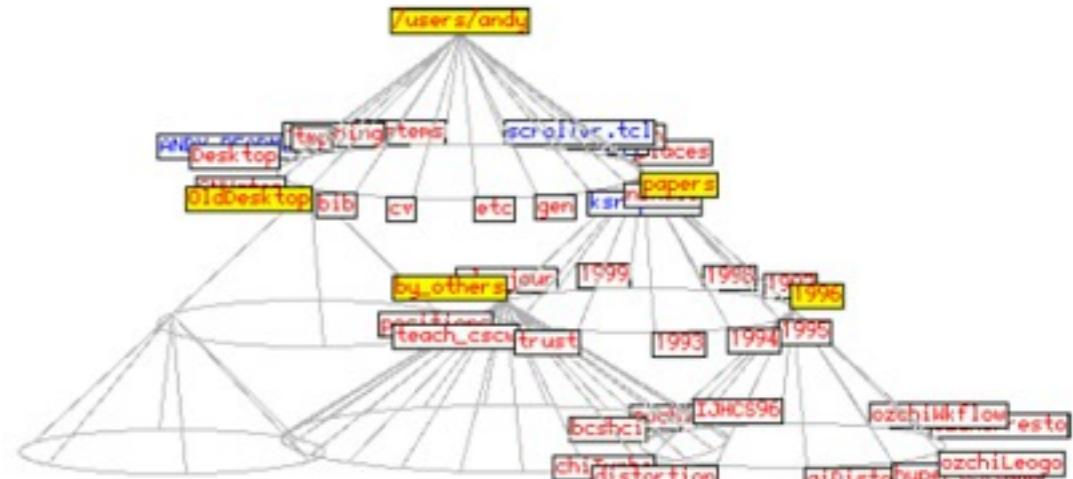
- Robertson et al. 1991
- Use depth to make more effective use of screen space
- Hierarchies laid out uniformly in three dimensions
- When a node is selected by a user the tree rotates to bring the node to the front
- Animation to make the users comprehend the rotation
- Problem: still clutter and occlusion





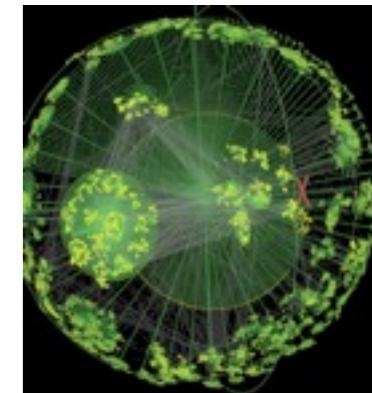
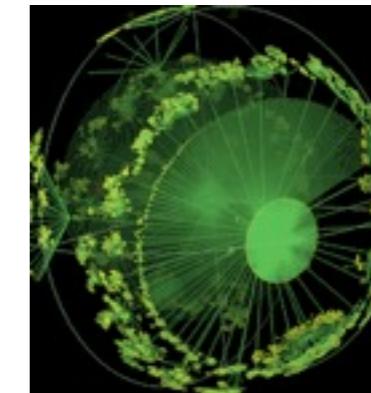
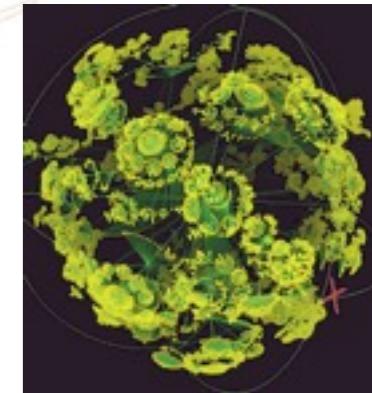
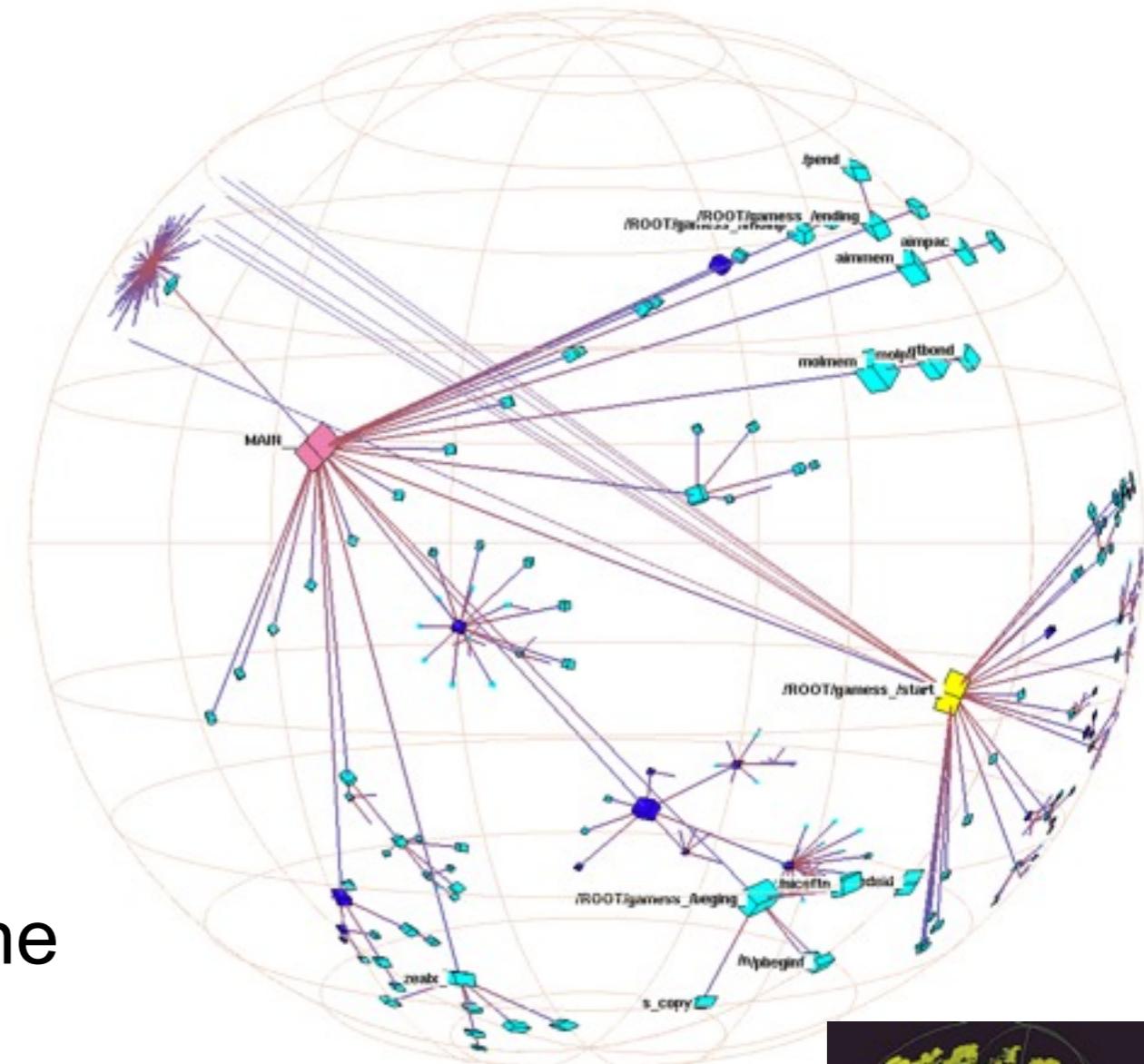
# Cone Tree

- Usability evaluation by Cockburn & McKenzie 2000
- Compare Cone Tree to conventional explorer-like 2D tree browser
- User test with 12 participants
- Independent variables: depth, density of tree, interface type
- Dependent variables: task-completion time, user preference
- Results
  - Users were slower in locating data using the Cone Tree
  - Performance deteriorated rapidly with a growing branching factor
  - But: participants clearly preferred the Cone Tree...



# H3Viewer

- Munzner 1997
- H3Viewer supports interactive exploration of large graphs (> 100,000 edges)
- Graph is presented in 3D hyperbolic space
- Child nodes are distributed on the surface of a hemisphere
- Users can drag and rotate graph
- Java 3D implementation and gallery: <http://www.caida.org/tools/visualization/walrus/>





# Treemap

- Johnson & Shneiderman 1992
- Basic idea
  - Map hierarchical data to rectangular 2D display area by recursively partitioning the screen into rectangular boxes representing nodes
  - Utilize 100% of the screen
- Less good for analyzing the topology of a tree
- Advantages
  - Very effective when focusing on leaf nodes and their attributes
  - More suitable for additional encoding via color, size, shape
  - Present large hierarchies on a single screen

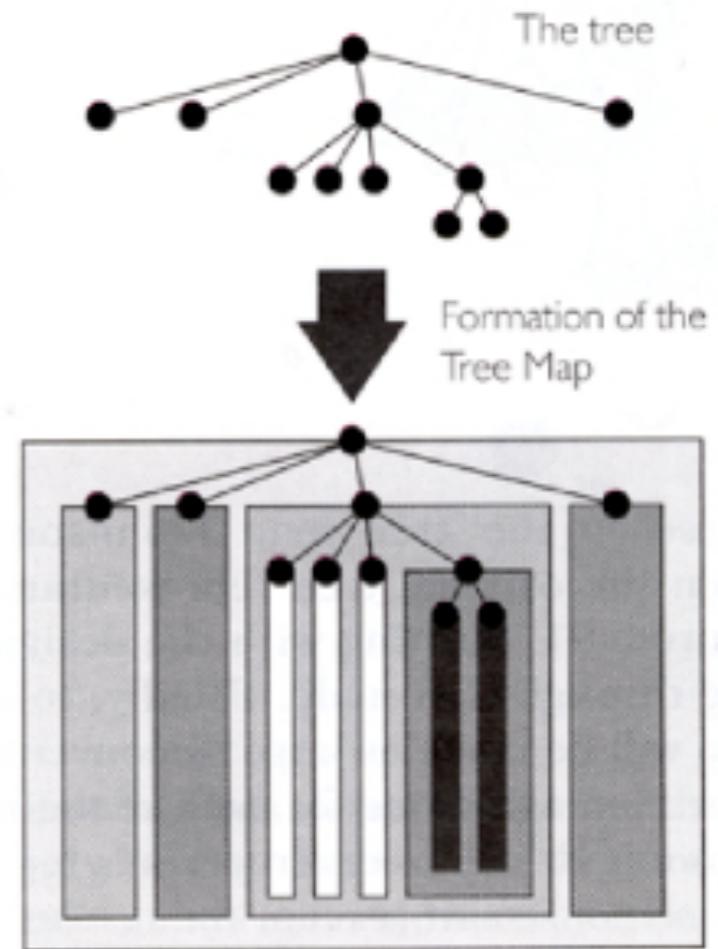
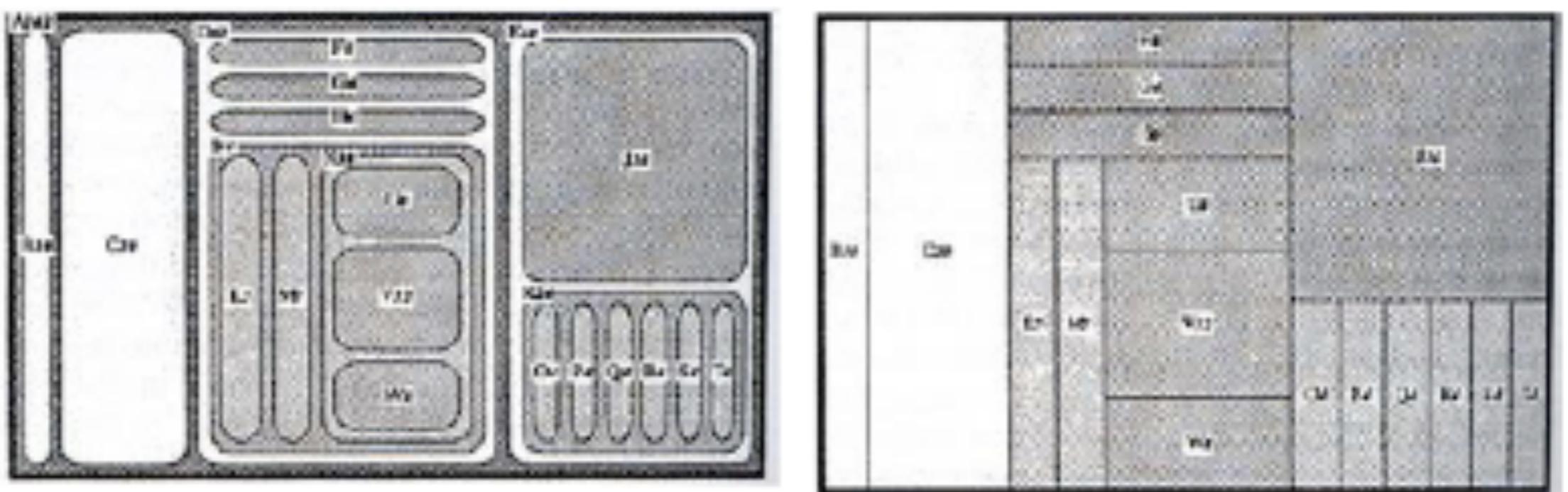


Image taken from  
Spence 2007

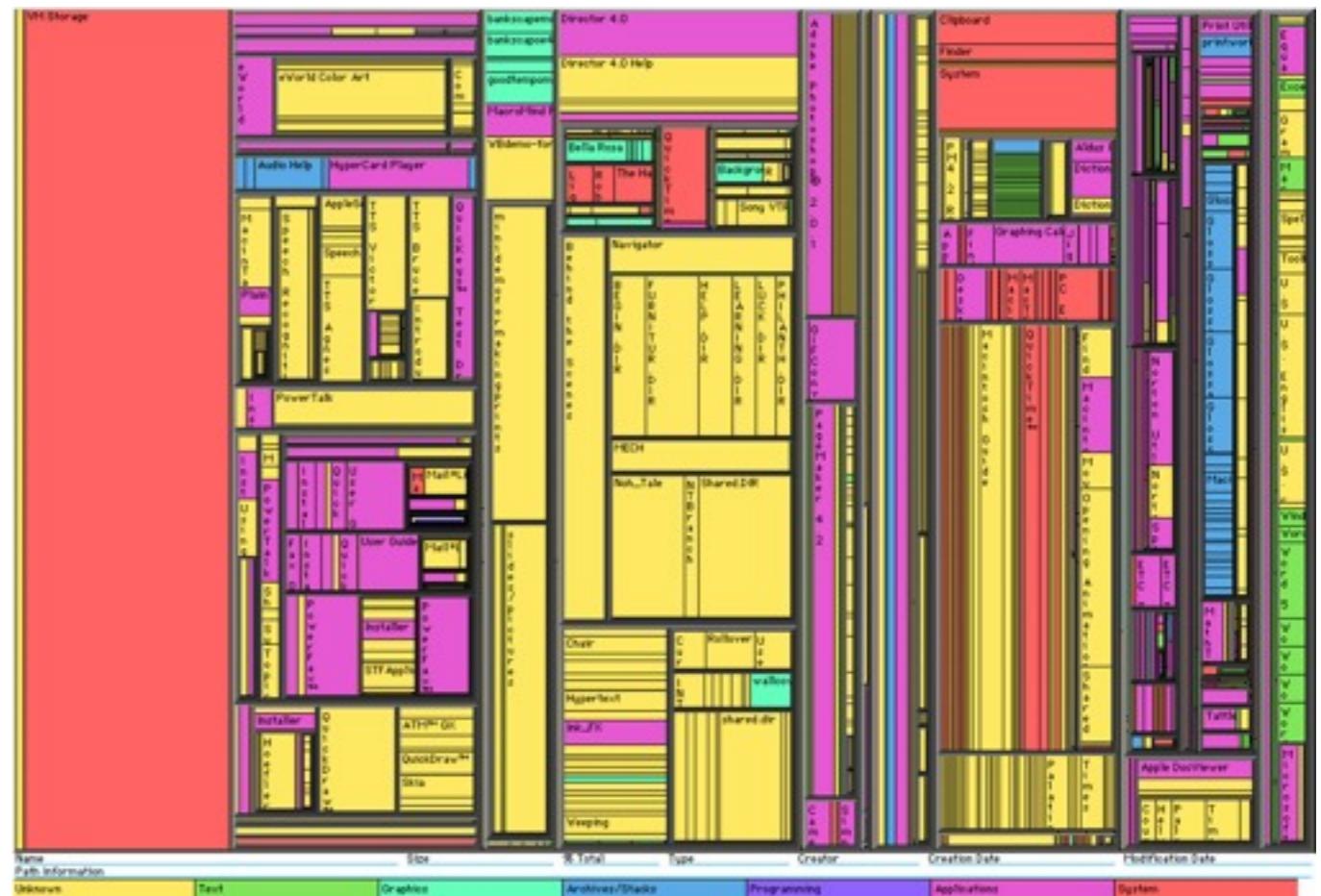
# Treemap

- Nested versus non-nested Treemaps



# Treemap

- Shneiderman 1992
- Slice and dice algorithm
  - Use parallel lines to divide a rectangle representing an item into smaller rectangles representing the item's children
  - Each child is allocated a size proportional to some property (additional encoding by color)
  - At each level of the hierarchy switch the orientation of the lines (vertical vs. horizontal)
- Example application: file browser
  - Size: file size, color: file type
  - Users can easily identify large file
  - Detect duplicate directories
  - ...



<ftp://ftpdim.uqac.ca/pub/ychirico/wvdr2002/nigay.pdf>

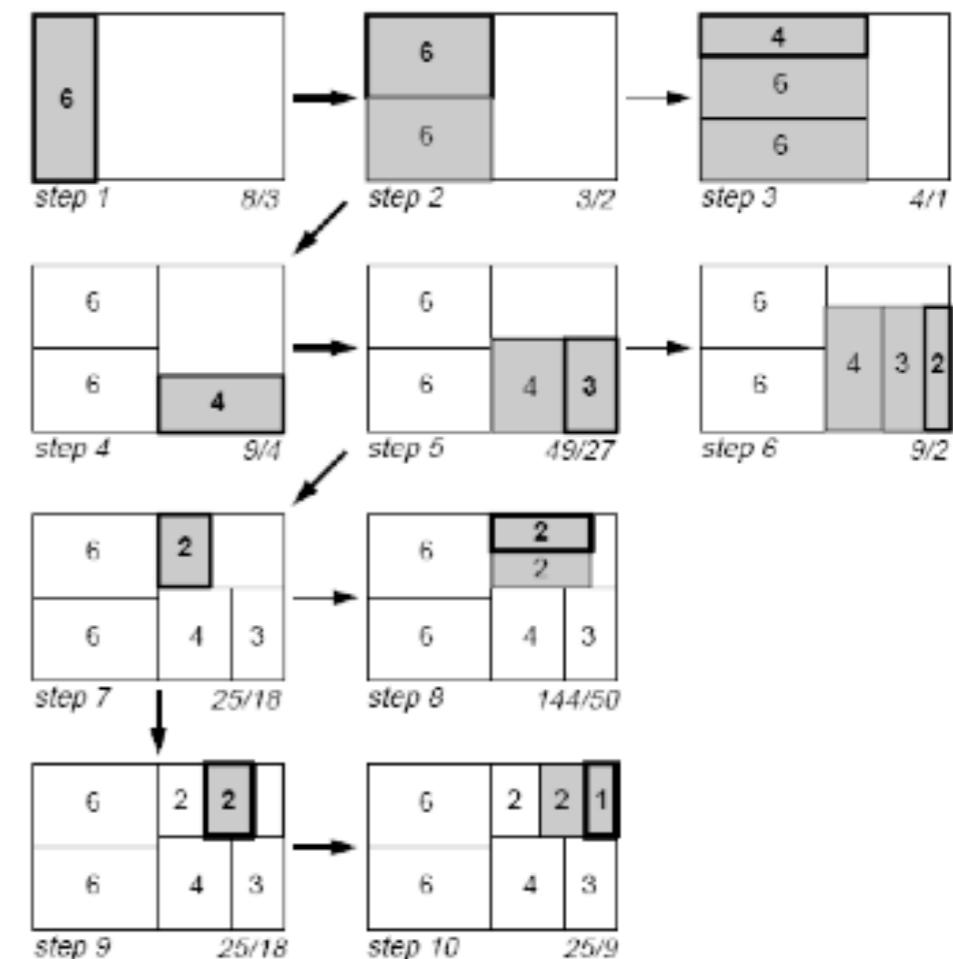
# Treemap: Discussion

- Problems with this layout?
- Creates layouts that contain many rectangles with a high aspect ratio
- Thin rectangles are hard to see, select, label and compare in size
- Which of the blue rectangles is bigger?

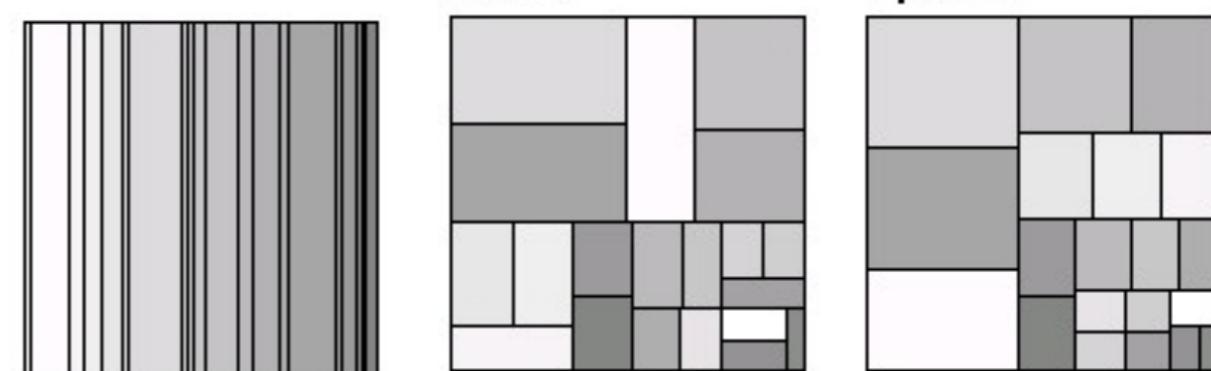


# Treemap

- Several algorithms to create more useful tree-maps by reducing the overall aspect ratios of the map rectangles
- Cluster algorithm (Wattenberg 1999):
  - employ both vertical and horizontal partitions at each level of the hierarchy
- Squarified algorithm (Bruls et al. 2000)
  - Sorts and adds the input rectangles ordered by size
- Problem of both algorithms
  - Changes in the data set can cause dramatic layout changes (hard to track items given dynamic data)
  - Given ordering of items is not preserved (as indicated by shading)

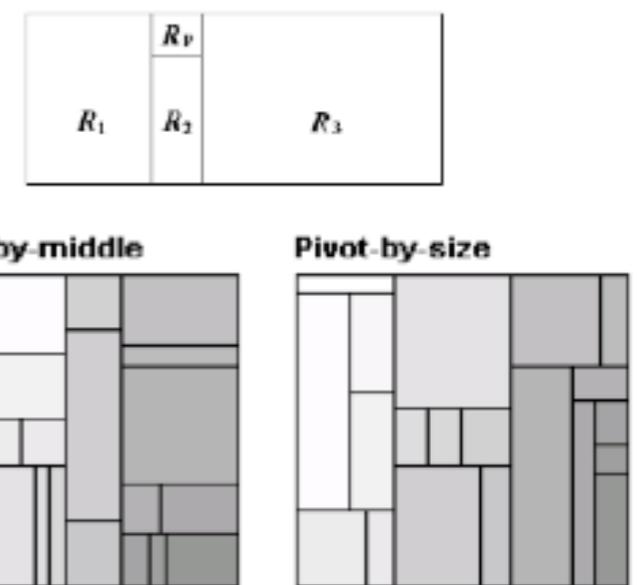


Subdivision algorithm for squarified algorithm  
(Bruls et al. 2000)



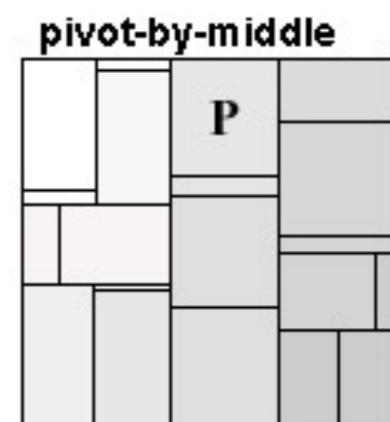
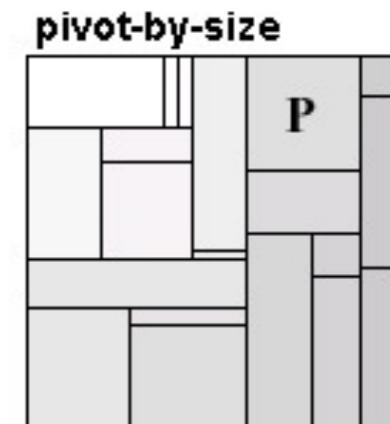
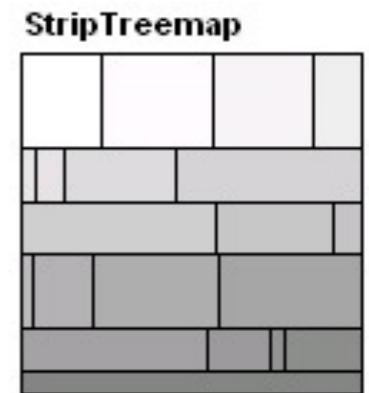
# Ordered Treemap

- Seek compromise between smooth updates and low aspect ratios
- Items are given as a list ordered by index and have varied areas
- Items that are next to each other in the given order should be approximately adjacent in the tree-map
- Shneiderman & Wattenberg 2001
- Pivot-by-size & Pivot-by-middle
  - Partition area into 4 regions
  - Pick pivot element  $R_p$ 
    - Size: largest item
    - Middle: middle item
  - Depending on the aspect ratio of  $R$ , place  $R_p$  in horizontal oder vertical middle
  - $R_1$ : items earlier in the list than pivot (sublist L1)
  - $R_2$ : items in list before  $R_3$  such that their overall size makes  $R_p$  have aspect ratio closest to 1 (sublists L2, and L3)
  - Apply steps recursively for areas  $R_1$ ,  $R_2$ , and  $R_3$



# Ordered Treemap

- Strip treemap - Bederson & Shneiderman 2002
- Modification of squarified algorithm
- Produces better readability than basic ordered treemap algorithms and comparable aspect ratios (only slightly worse than unordered squarified algorithm)
- Rectangle is filled stepwise with strips
- Strip is filled stepwise with rectangles as long as the average aspect ratio of the strip decreases or stays the same
- Otherwise a new strip is added



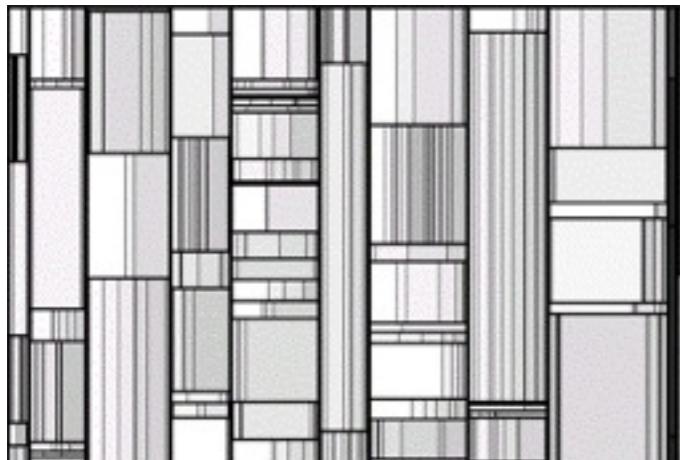
# Ordered Treemap

- Test with several generated data sets
- Table shows results for three levels of hierarchy and eight items at each level
- 100 trials of 100 steps each
- Comparing the algorithms by average aspect ratio and average layout distance change (how much do rectangles move as data is updated) and readability (how easy it is to visually scan a layout to find a particular item)
- Tradeoff between low aspect ratios and smooth updates!

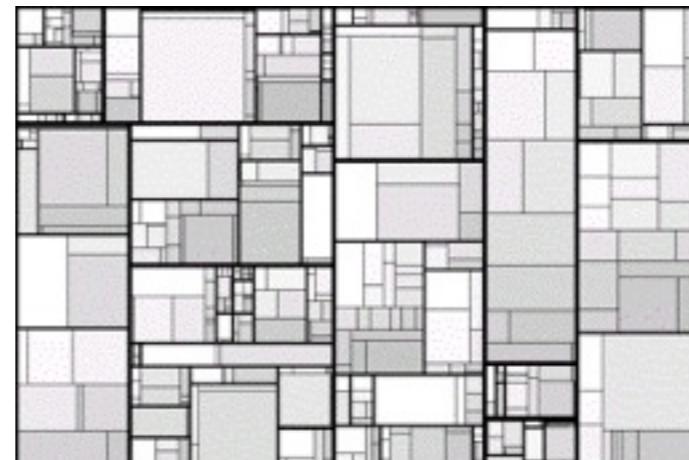
Algorithm	Aspect Ratio	Change	Readability
Slice-and-dice	26.10	0.46	1.0
Pivot-by-middle	3.58	1.21	0.42
Pivot-by-size	3.31	4.14	0.33
Pivot-by-split	3.00	2.37	0.35
Strip	2.83	1.09	0.51
Cluster	1.79	7.67	0.26
Squarified	1.74	8.27	0.26

# Ordered Treemap

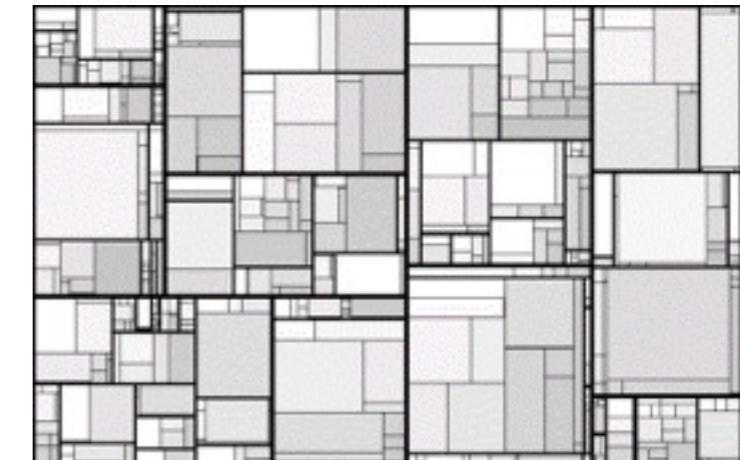
- Applying the algorithms to real-world data - confirmed prior test results
- Set of 535 publicly traded companies, market capitalization as the size attribute
- Gray scale indicates ordering within each industry group that is the last level of hierarchy in this data set



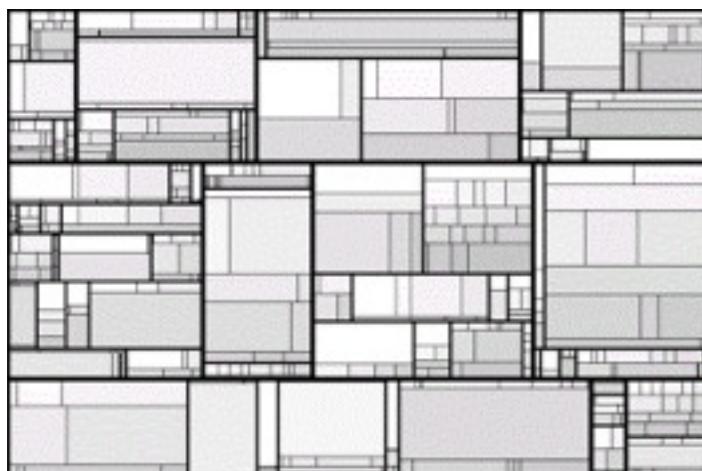
Slice-and-dice layout



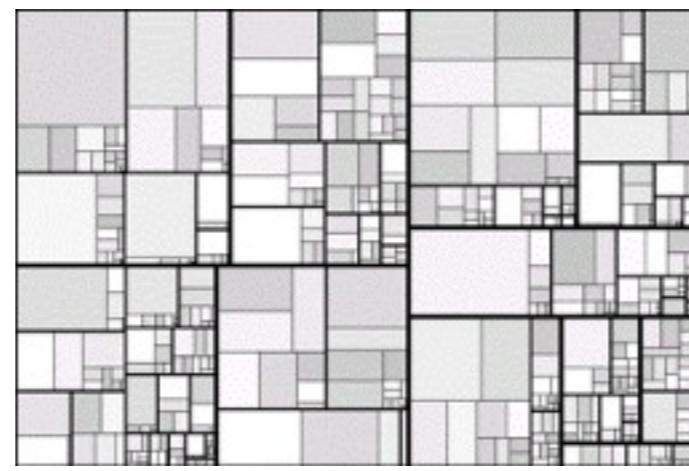
Pivot-by-middle layout.



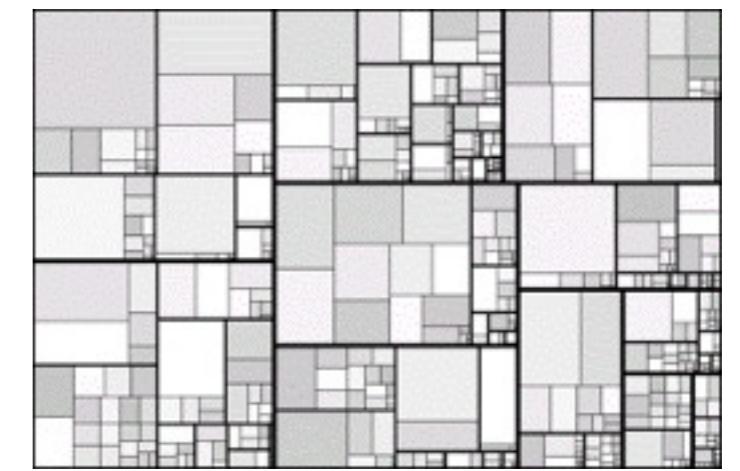
Pivot-by-size layout



Strip layout



Cluster layout



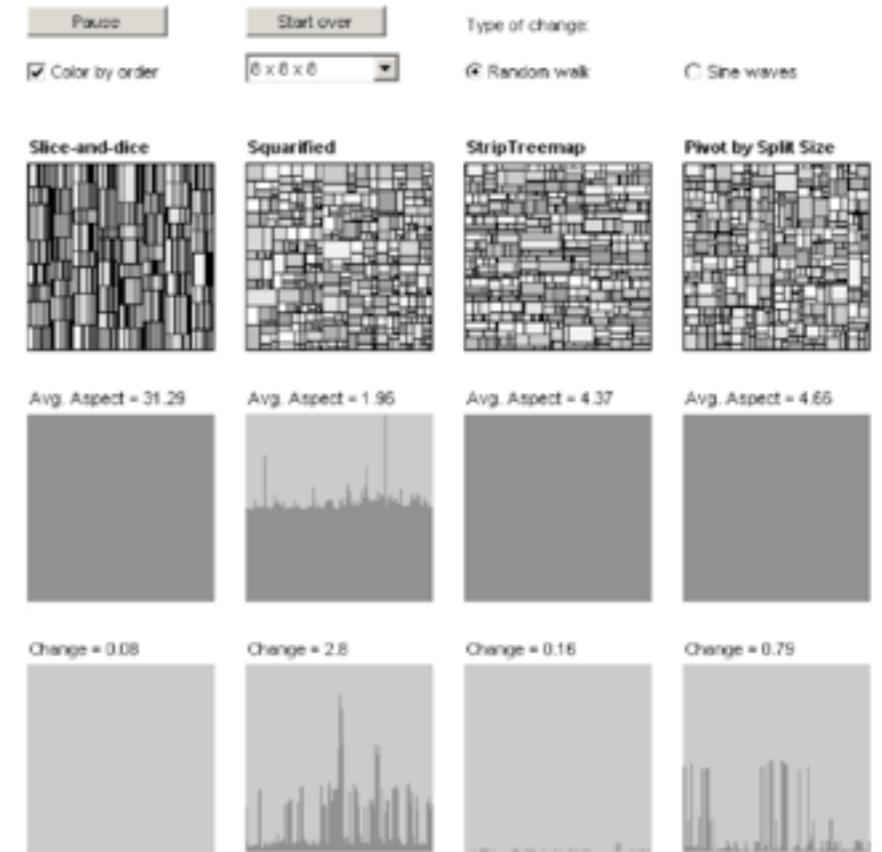
Squarefied layout.

# Ordered Treemap

- Compare algorithms
- [http://www.cs.umd.edu/hcil/treemap-history/java\\_algorithms/LayoutApplet.html](http://www.cs.umd.edu/hcil/treemap-history/java_algorithms/LayoutApplet.html)
- History of treemaps
- <http://www.cs.umd.edu/hcil/treemap-history/>
- Java 1.1 library for five Tree-map algorithms:
- <http://www.cs.umd.edu/hcil/treemap-history/Treemaps-Java-Algorithms.zip>

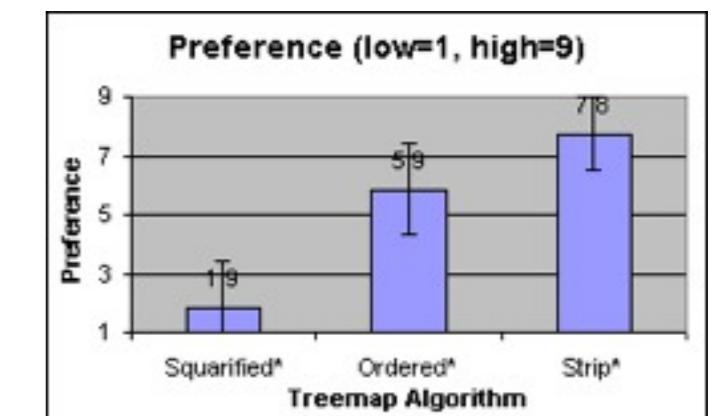
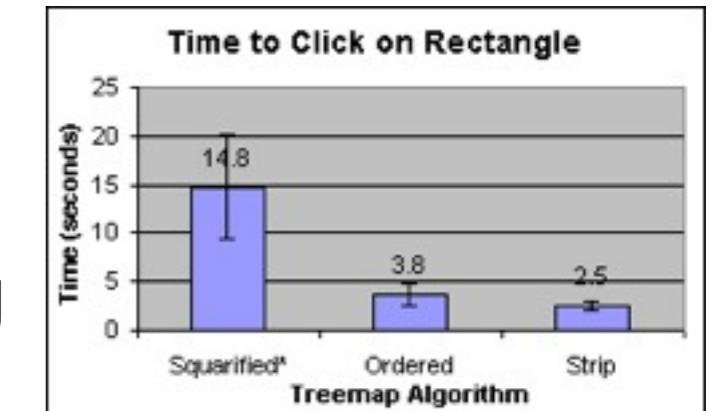
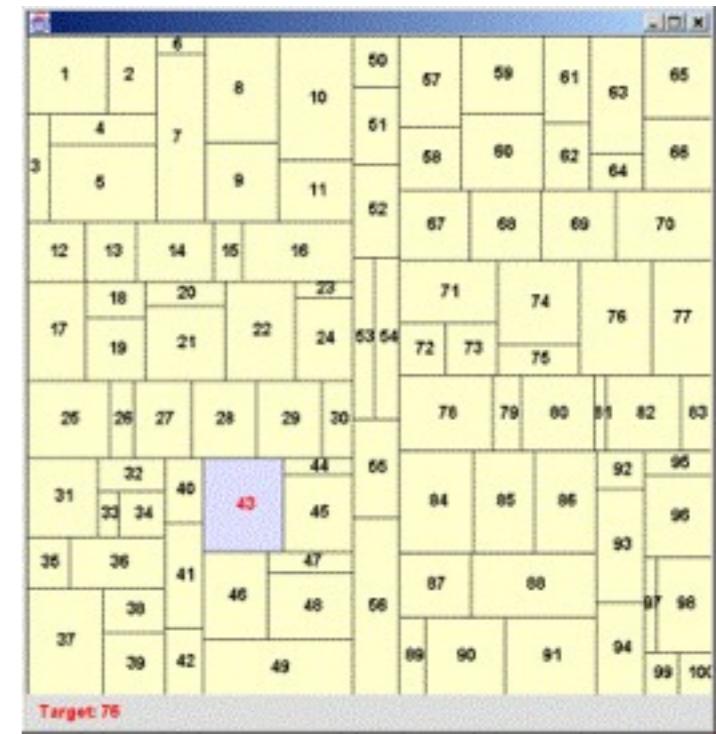
## Dynamic treemap layout comparison

- Martin Wattenberg, [wi@bewitched.com](mailto:wi@bewitched.com)
- Ben Bederson, (University of Maryland, [Human-Computer Interaction Lab](#))



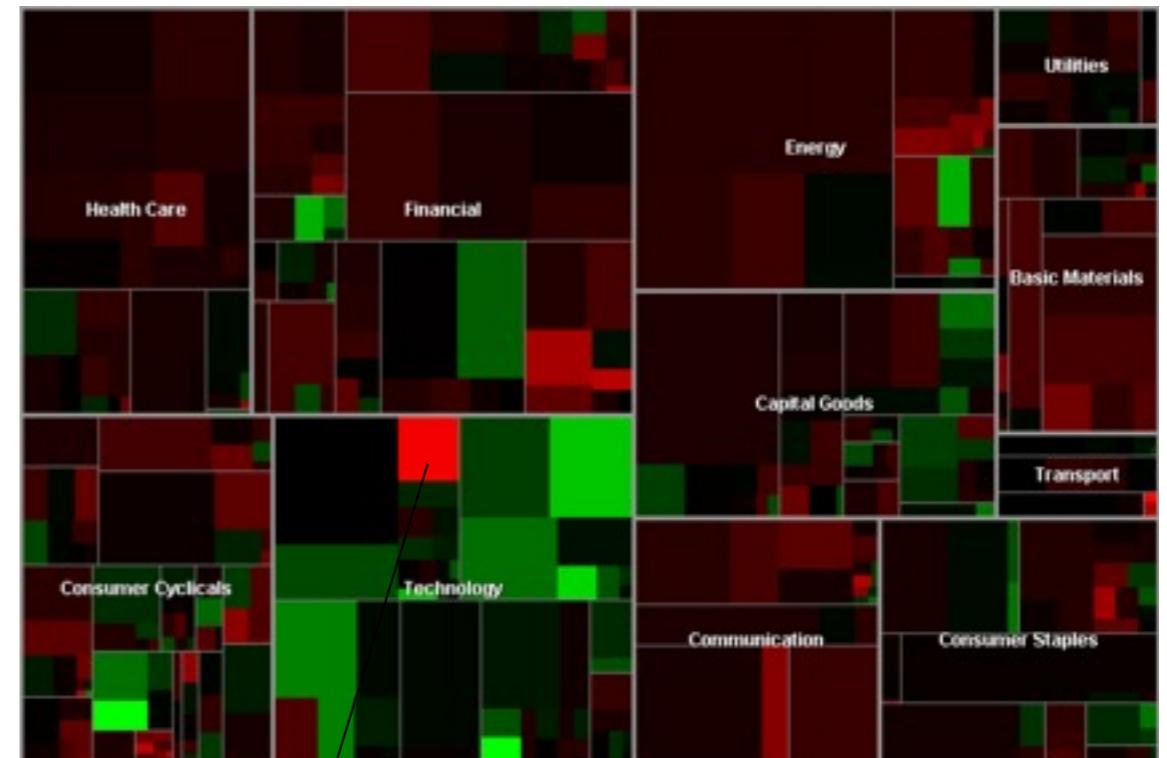
# Ordered Treemap

- Bederson et al. 2002
- User study of layout readability
- Compared the squarified, pivot-based, and strip treemap algorithms
- 20 Participants had to identify a specific rectangle by clicking on the rectangle with the requested numerical ID
- Repeated-measures design
- Independent variable: treemap algorithm
- Dependent variable: time, subjective user rating
- Time: significant difference between squarified algorithm and the other two
- Preference: significant difference between all three algorithms
- Validates readability metric used



# Map of the Market

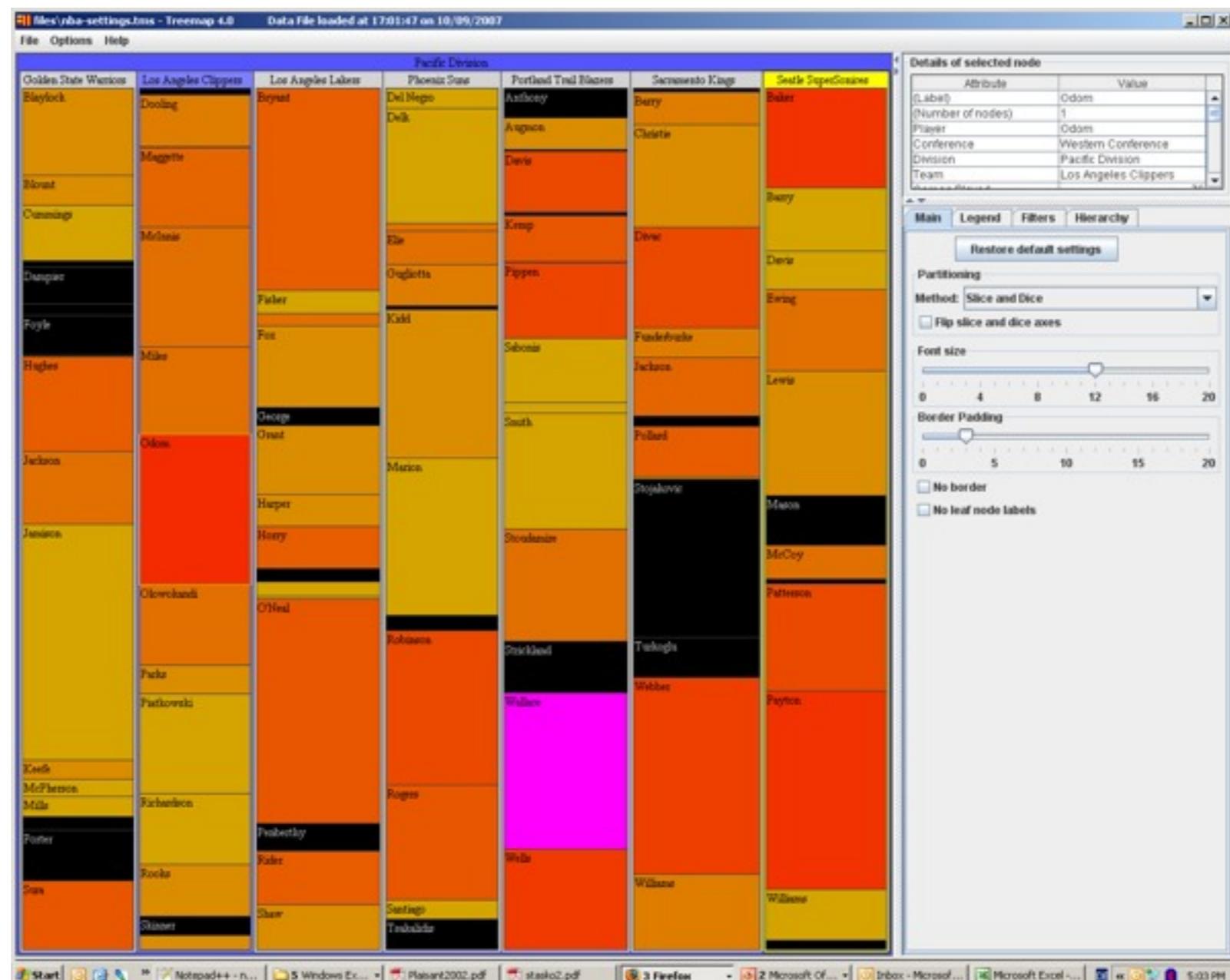
- Wattenberg 1999
- Cluster treemap to reduce overall aspect ratios
- <http://www.smartmoney.com/marketmap/>
- 500 stocks updated every 15 minutes
- Each rectangle represents a company
  - Size: company's market capitalization
  - Color: price performance
- Double-ended multiple hue color coding
  - Green: stock price is up
  - Red: stock price is down
  - Black: neutral, no change
- Detailed information on-demand
- Demo if time..



SAP Pays \$6.8 Billion for Business Objects

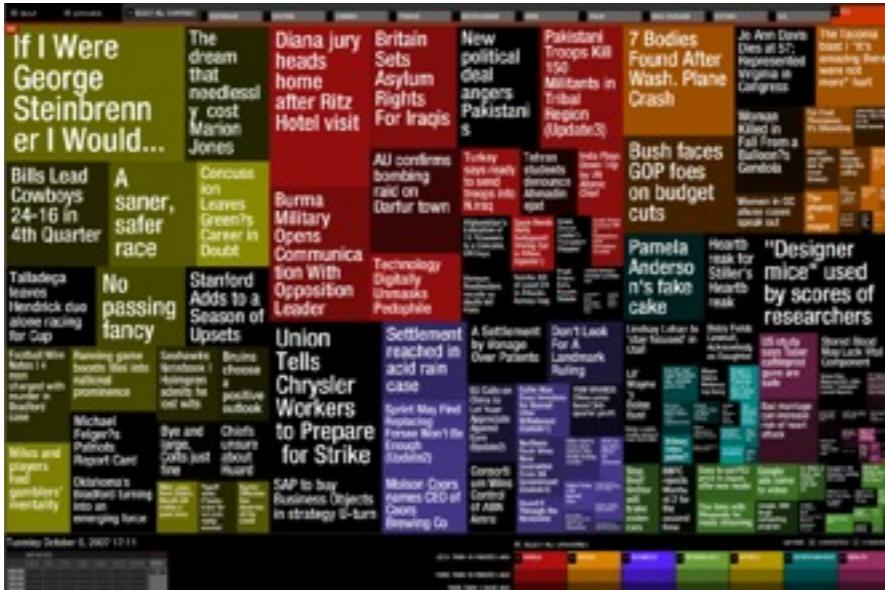
# Treemap 4.1

- Human-Computer Interaction Lab – University of Maryland
- Applet: <http://www.cs.umd.edu/hcil/treemap/index.shtml>



# Other Treemaps Online

NewsMap



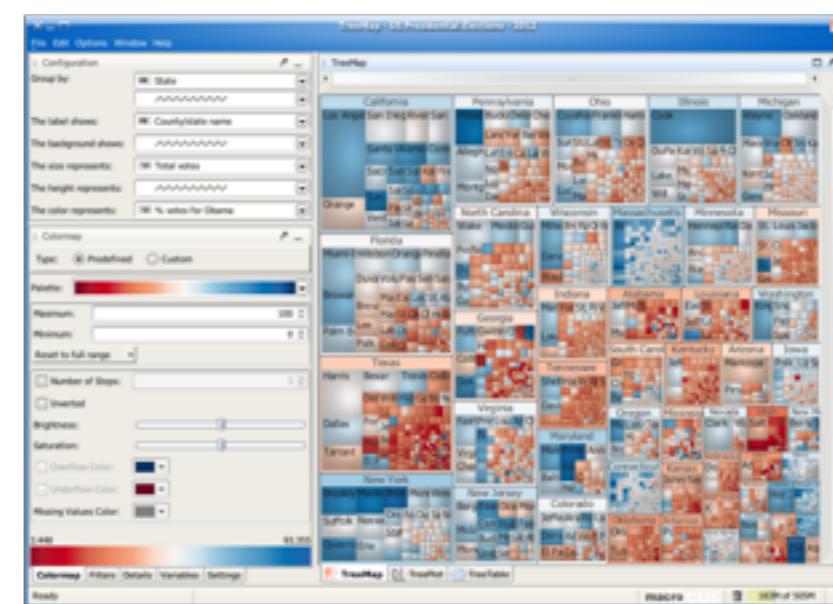
Peet's Coffee: Coffee Selector



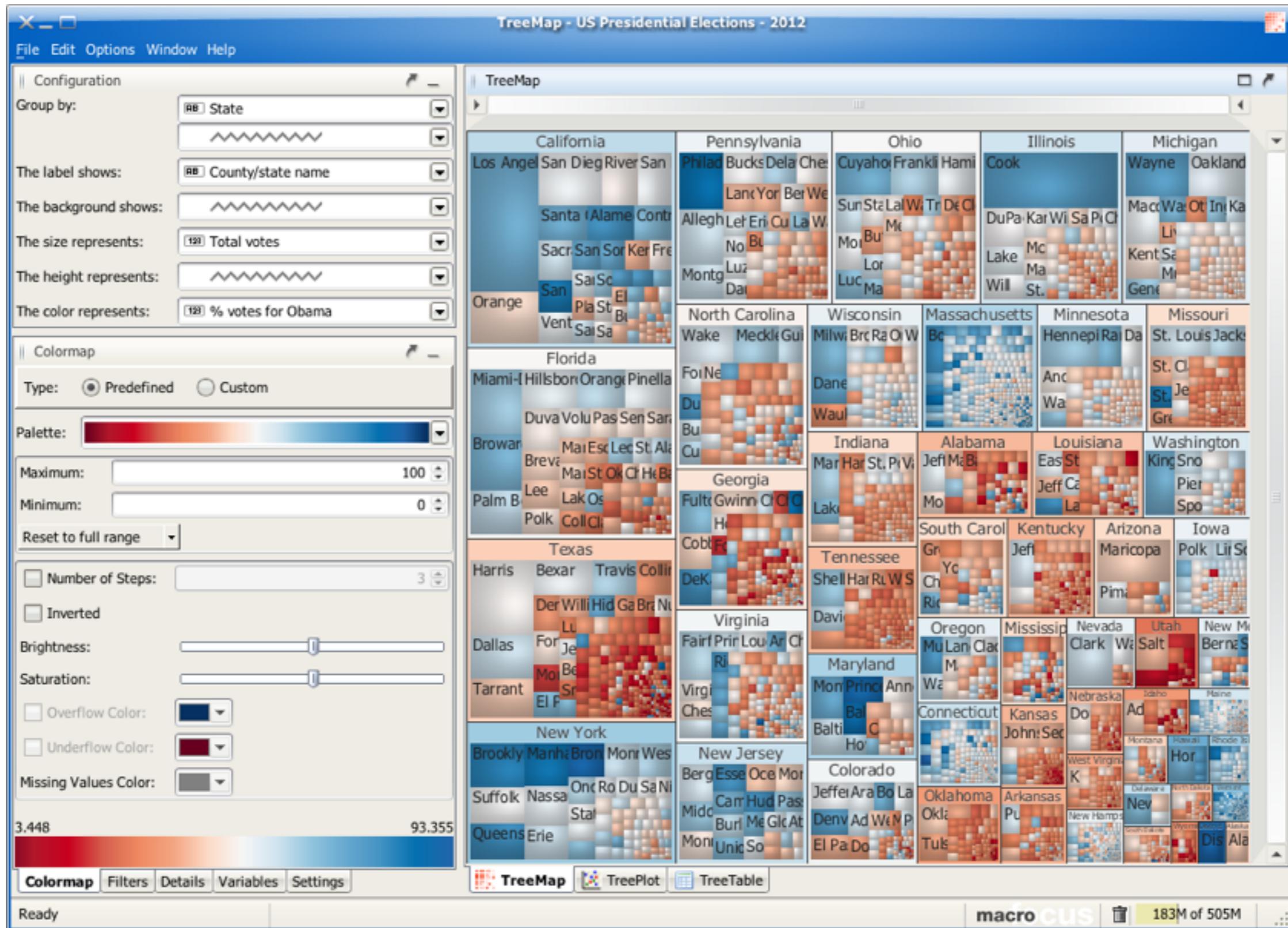
2012 White House Budget Proposal



US Presidential Elections 2012



# US Presidential Elections 2012



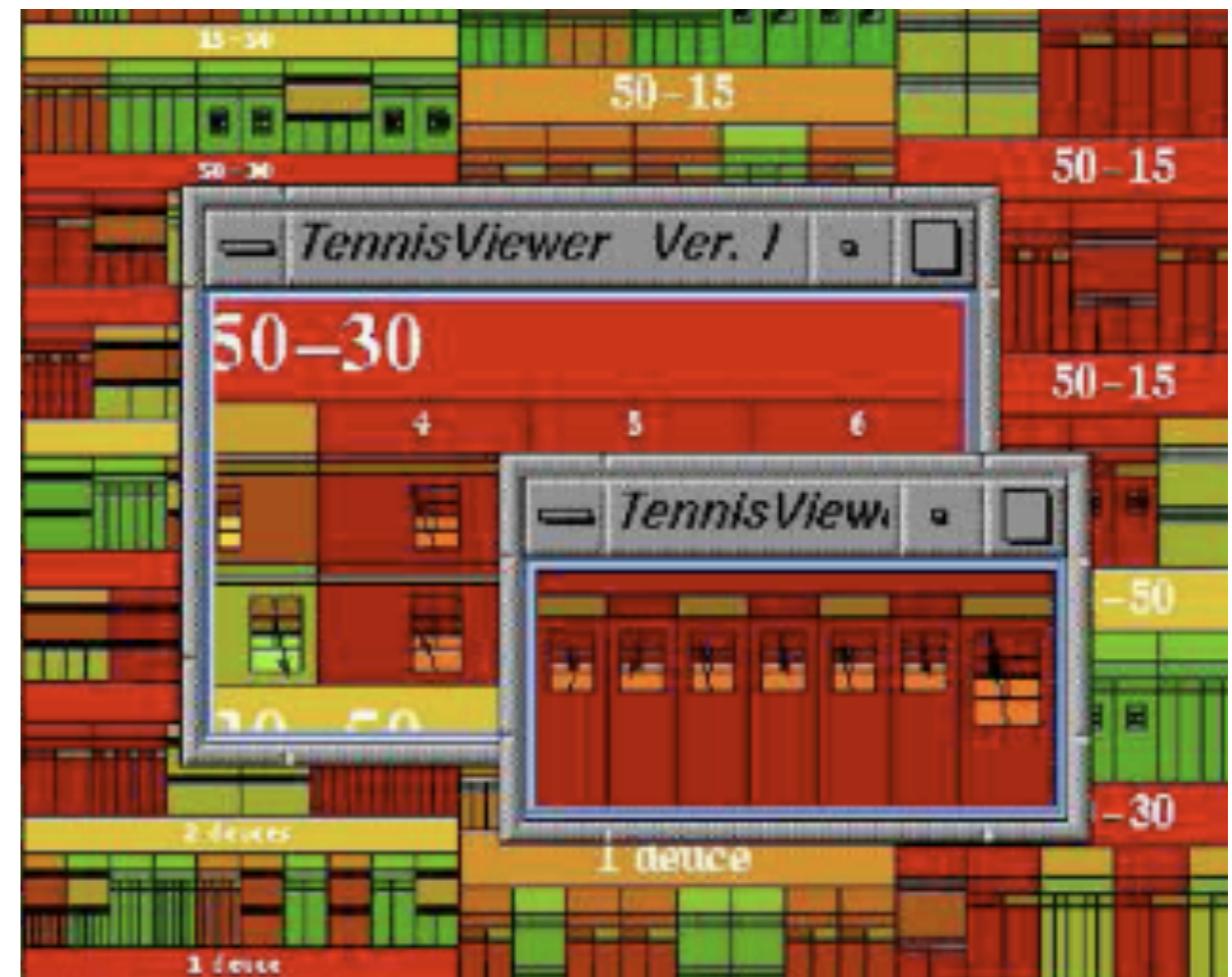
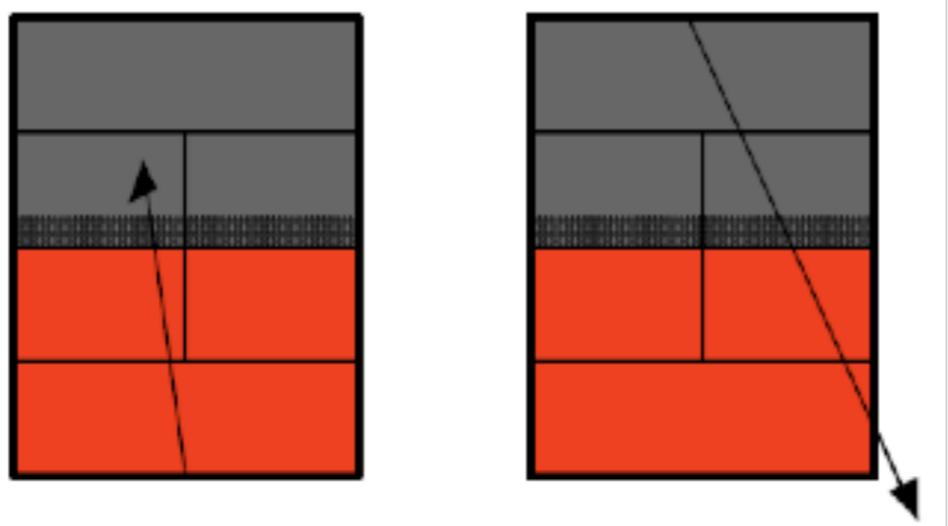
# TennisViewer

- Jin & Banks 1997
- Visualize a tennis match using a treemap
- Match tree
  - Root node – the tennis match
  - Match node subdivides horizontally into sets
  - A set subdivides vertically into games
  - A game subdivides horizontally into points
- Color mapping of rectangles show node ownership (who won what?)
- Translucent child rectangles are layered over parent rectangles



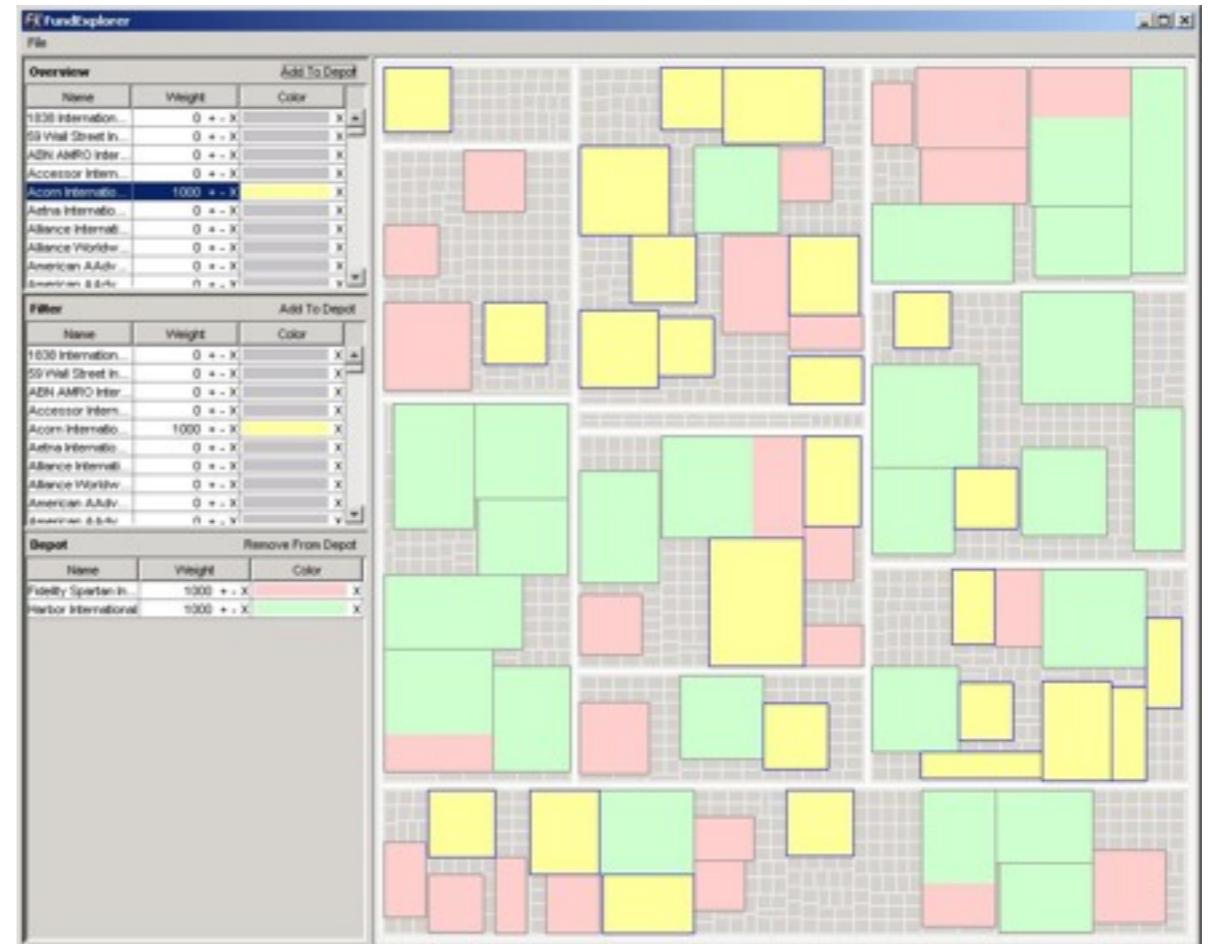
# TennisViewer

- Magic Lens to explore ball traces
- Example: the return of a service goes out of bounds



# FundExplorer

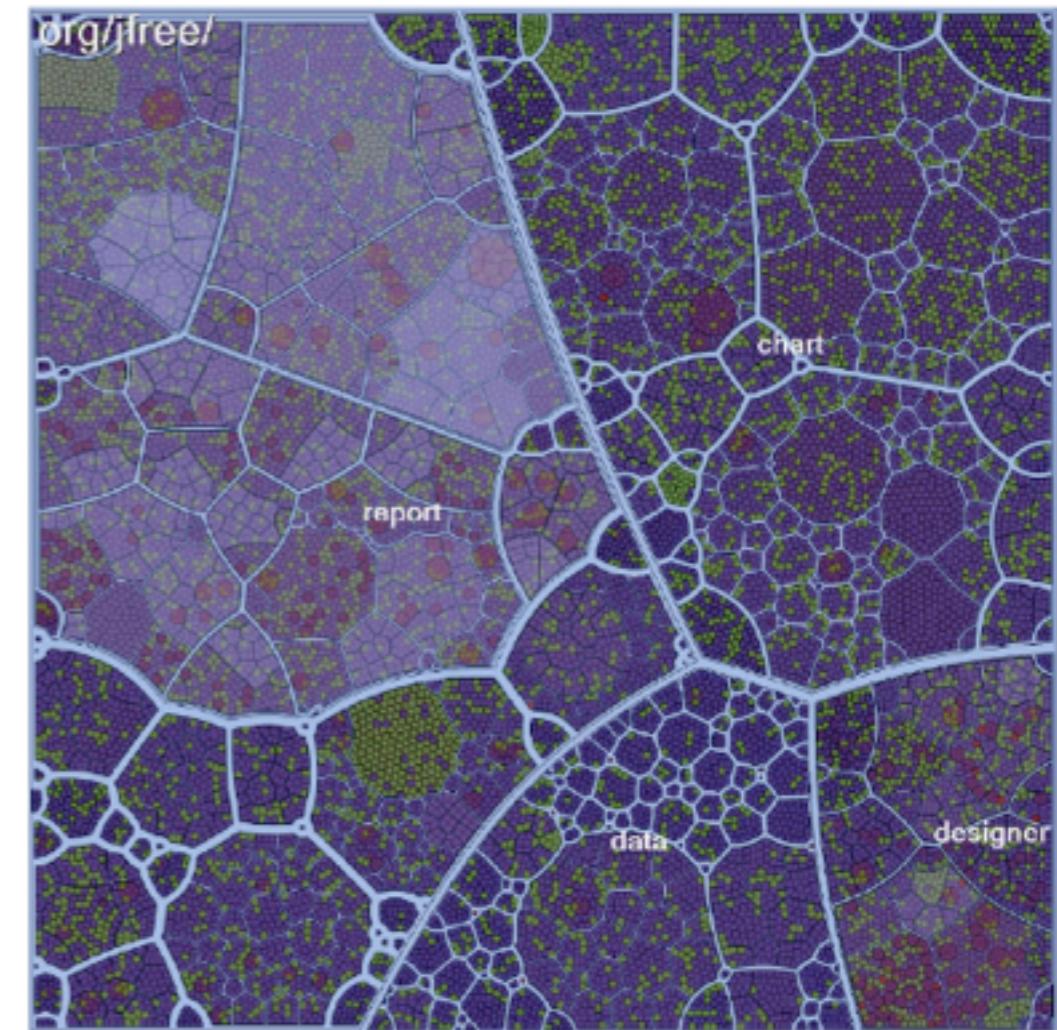
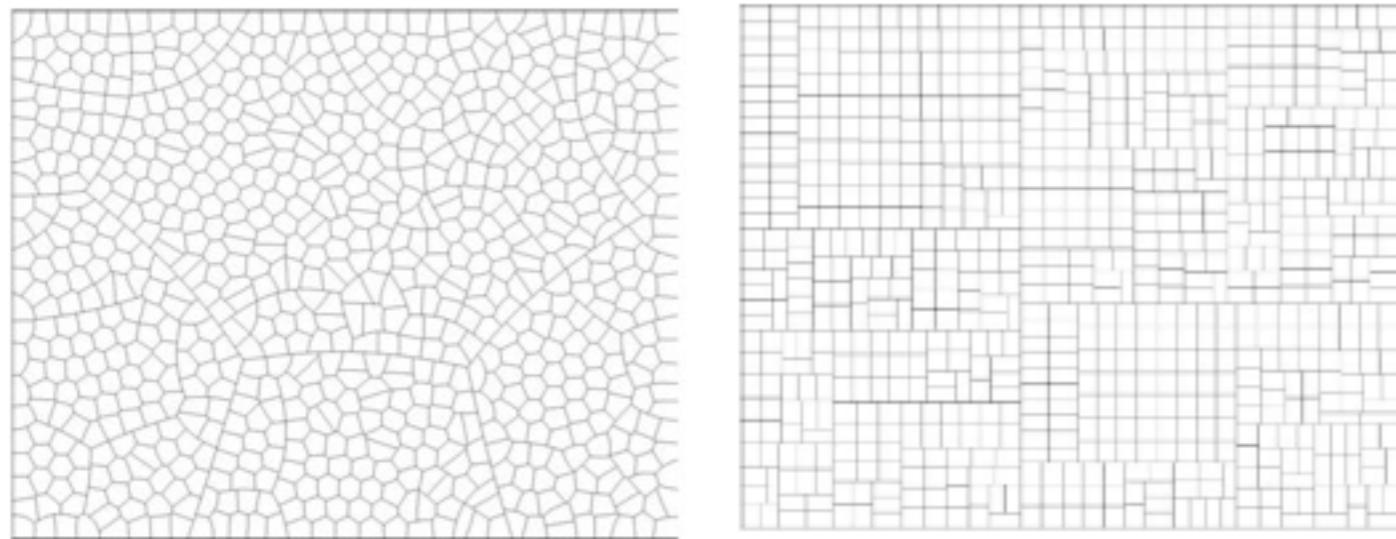
- Csallner et al. 2003
- To support the diversification of mutual fund portfolios, i.e. how to find funds with little overlap in their investments
- Also show stocks with zero investment





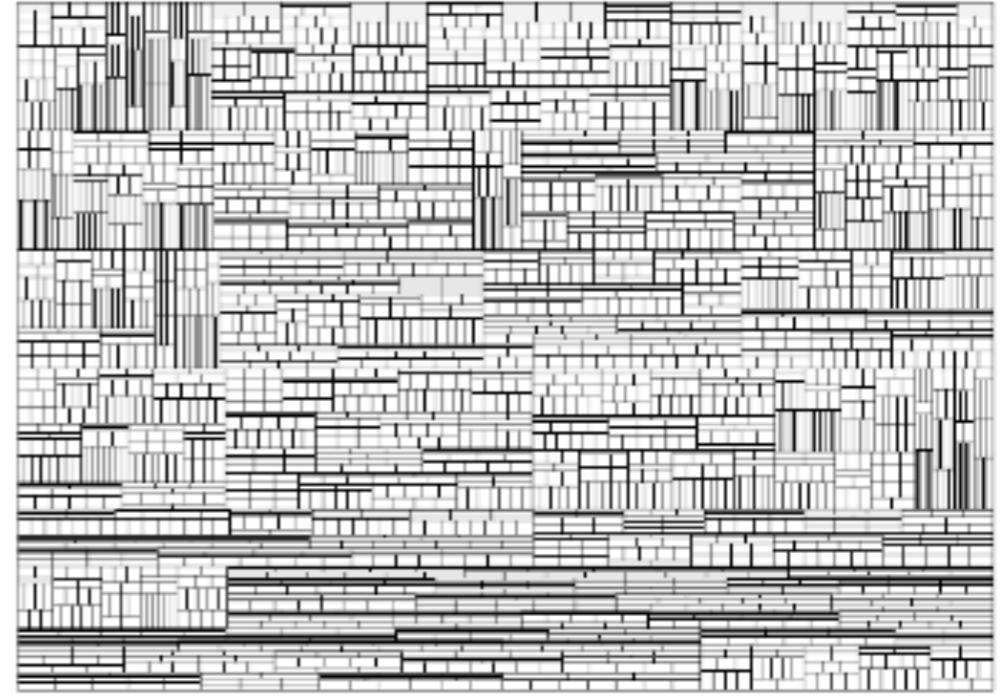
# Voronoi Treemap

- Balzer et al. 2005
- Treemap consisting of arbitrary polygons instead of rectangles
  - Aspect ratio of polygons converges to 1
  - Polygons are distinguishable due to the irregular shapes
  - Avoid that edges of different objects run into each other



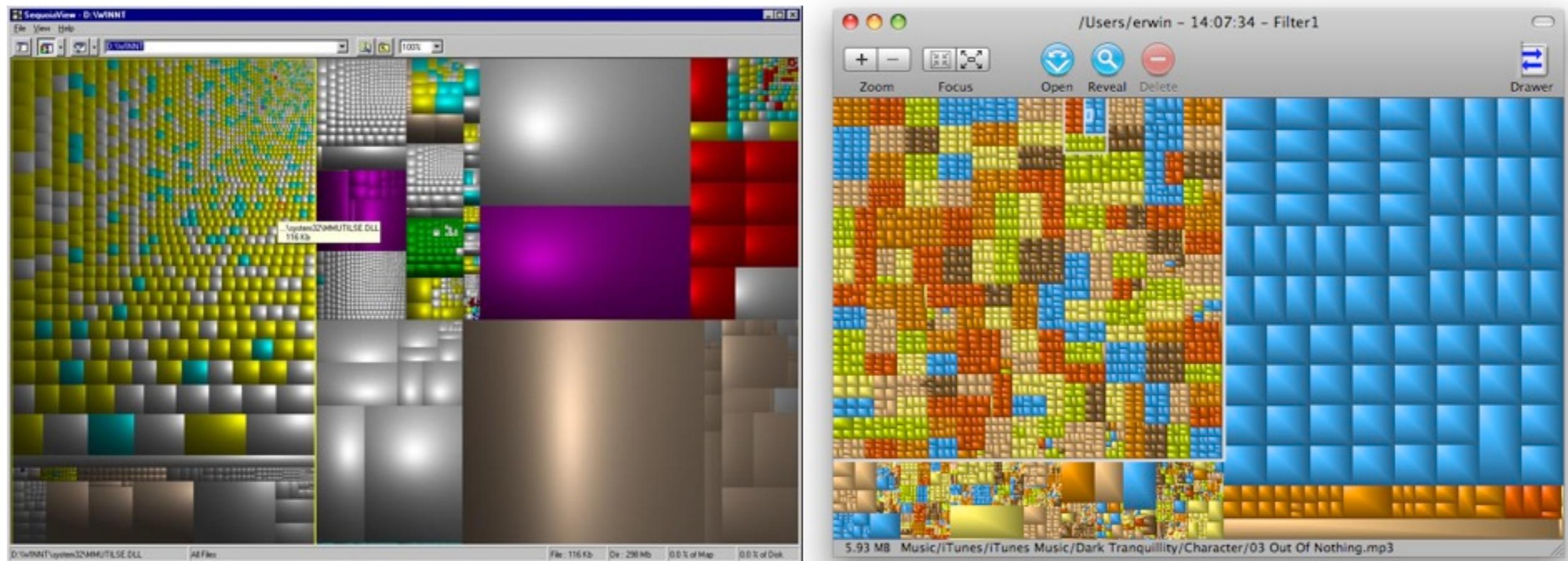
# Cushion Treemap

- Wijk & van de Wetering 1999
- Treemaps usually fall short to visualize the structure of the tree
- Worst case: a balanced tree, where each parent has the same number of children and each leaf the same size
- Outcome: regular grid
- Nested treemap may reduce this problem, but:
  - Margins require screen space
  - Deeply nested trees are difficult to read
- Idea: add shading and texture to help convey the structure of the tree



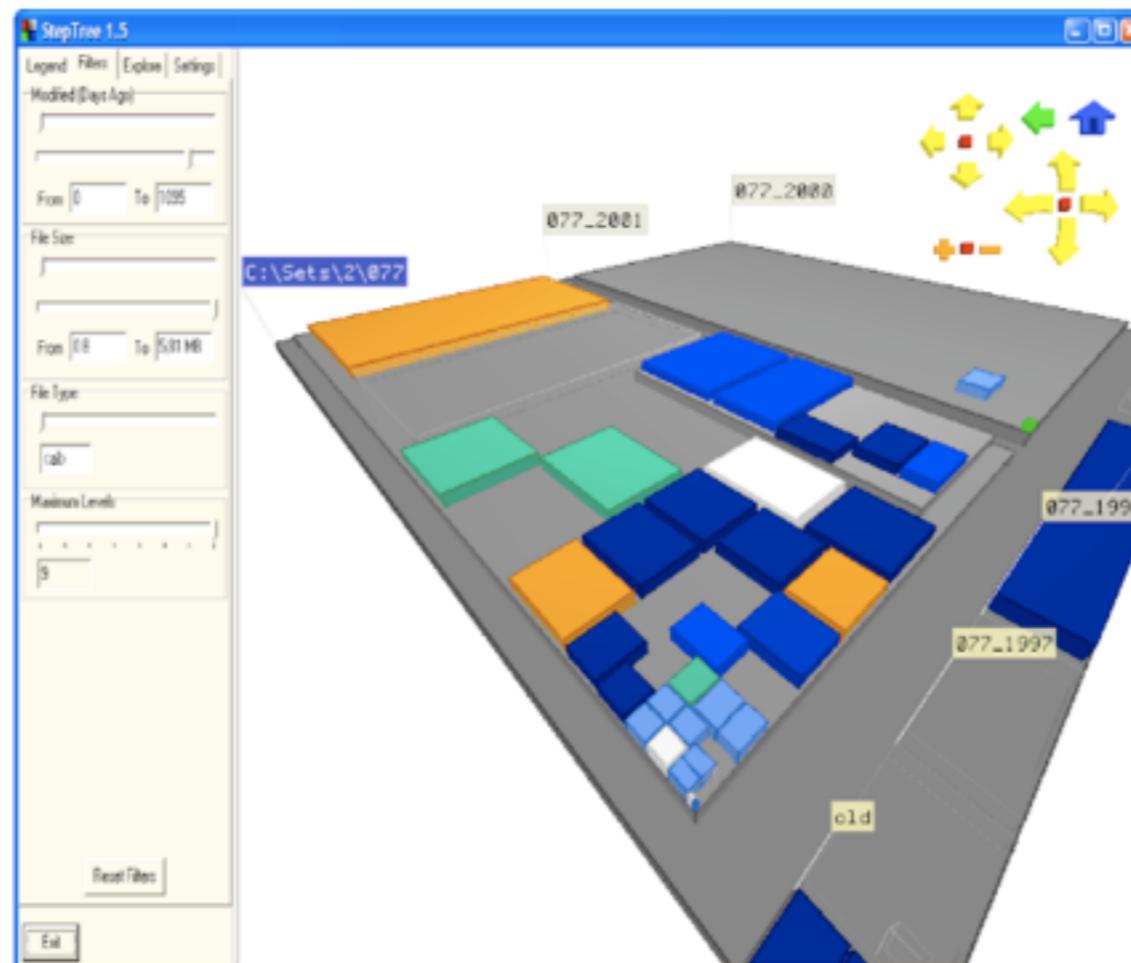
# Some really useful Cushion Treemaps

- SequoiaView [http://w3.win.tue.nl/nl/onderzoek/onderzoek\\_informatica/visualization/sequoiaview/](http://w3.win.tue.nl/nl/onderzoek/onderzoek_informatica/visualization/sequoiaview/)
- GrandPerspective <http://grandperspectiv.sourceforge.net>
- Visualize the contents of your hard drive



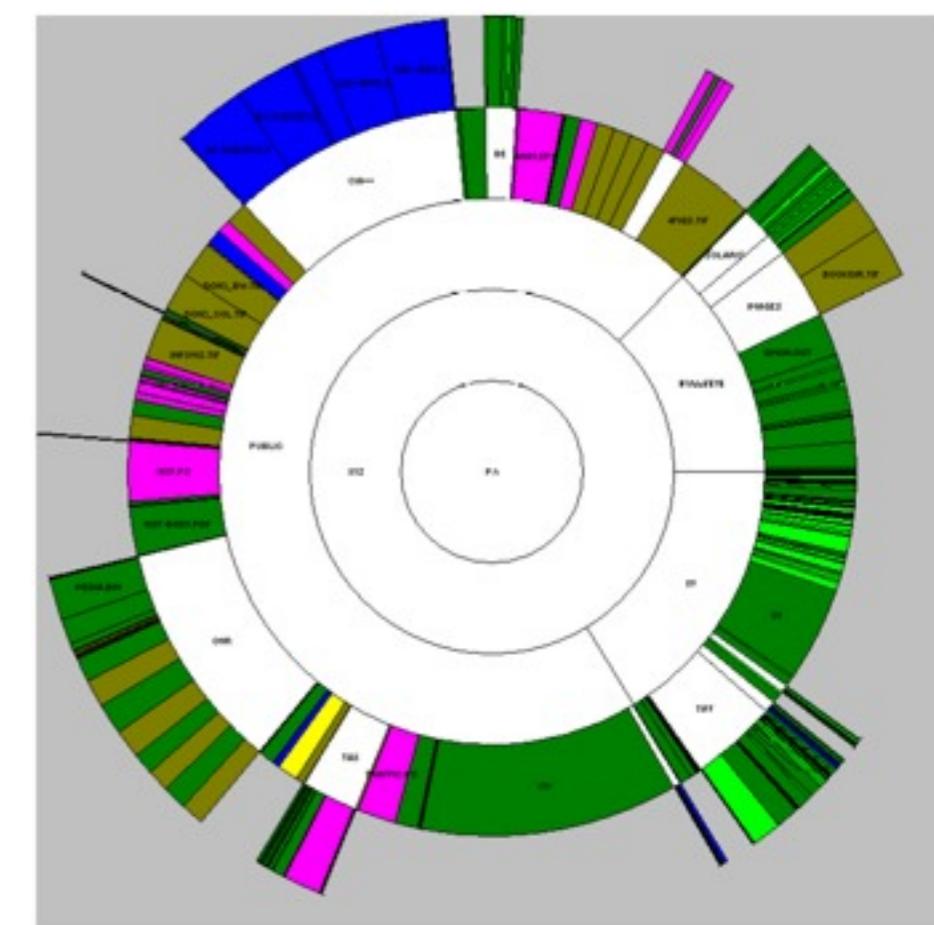
# StepTree

- Bladh et al. 2004
- Convey tree structure via third dimension
- <http://www.sm.luth.se/csee/csn/visualization/filesysvis.php>



# Sunburst

- Stasko & Zhang 2000
- Full circular visualization to give each element more space
- Navigating the tree should not lead to significant node position changes (e.g. hyperbolic browser)
- Three animated approaches to provide a focus area while maintaining context
  - Angular detail method
  - Detail outside method
  - Detail inside method
- Comparative evaluation of sunburst vs. treemap did not show significant differences in task completion times, but participants strongly preferred sunburst (Stasko et al. 2000)
- Radial visualizations may better depict the structure of the tree, but are not as space-efficient as treemaps (Movie)



Sunburst visualizing file structure

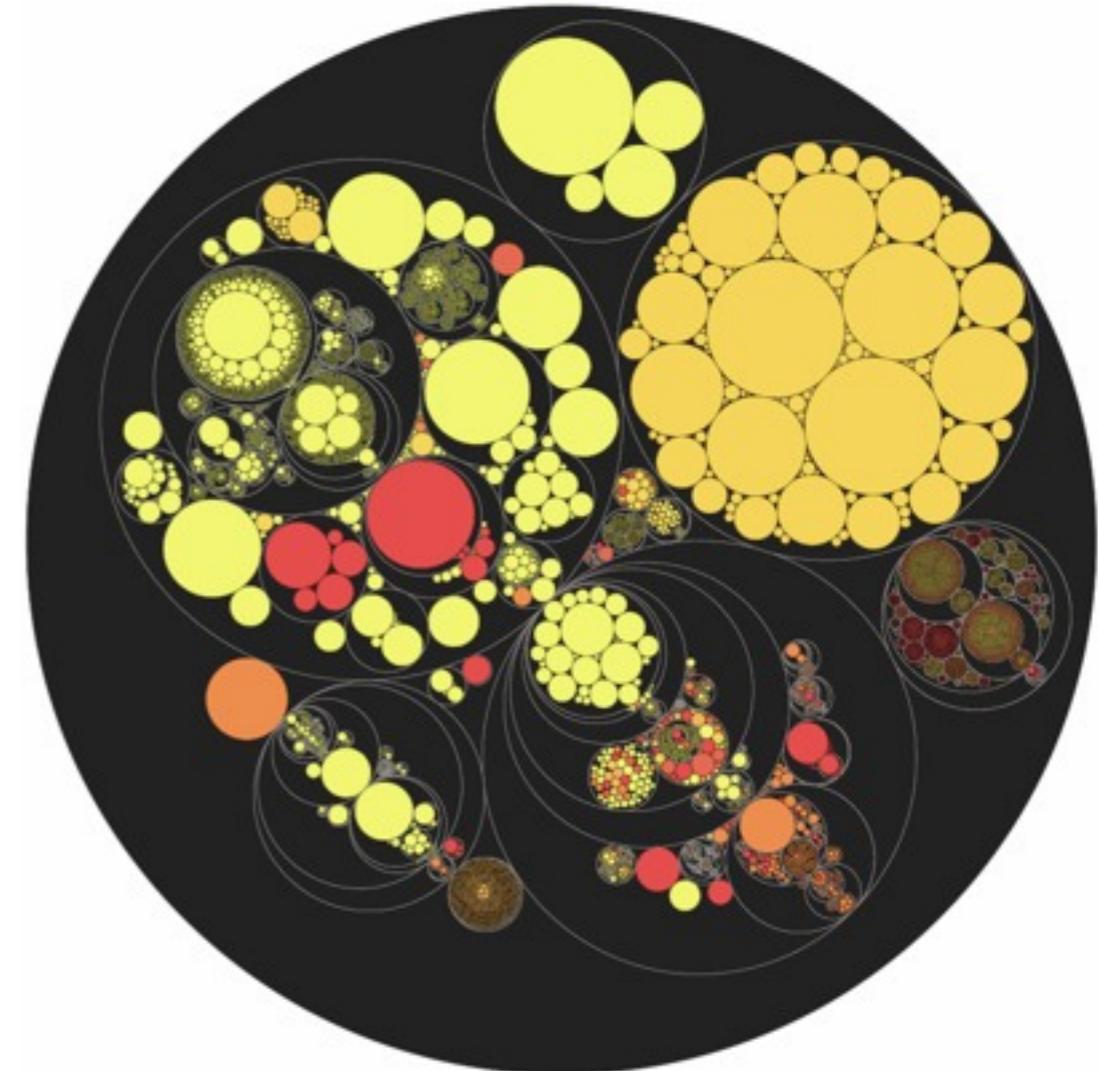
# Focus+Context Display and Navigation Techniques for Enhancing Radial, Space-Filling Hierarchy Visualizations

John Stasko and Eugene Zhang

College of Computing and GVU Center  
Georgia Institute of Technology

# Pebbles - Circular Treemaps

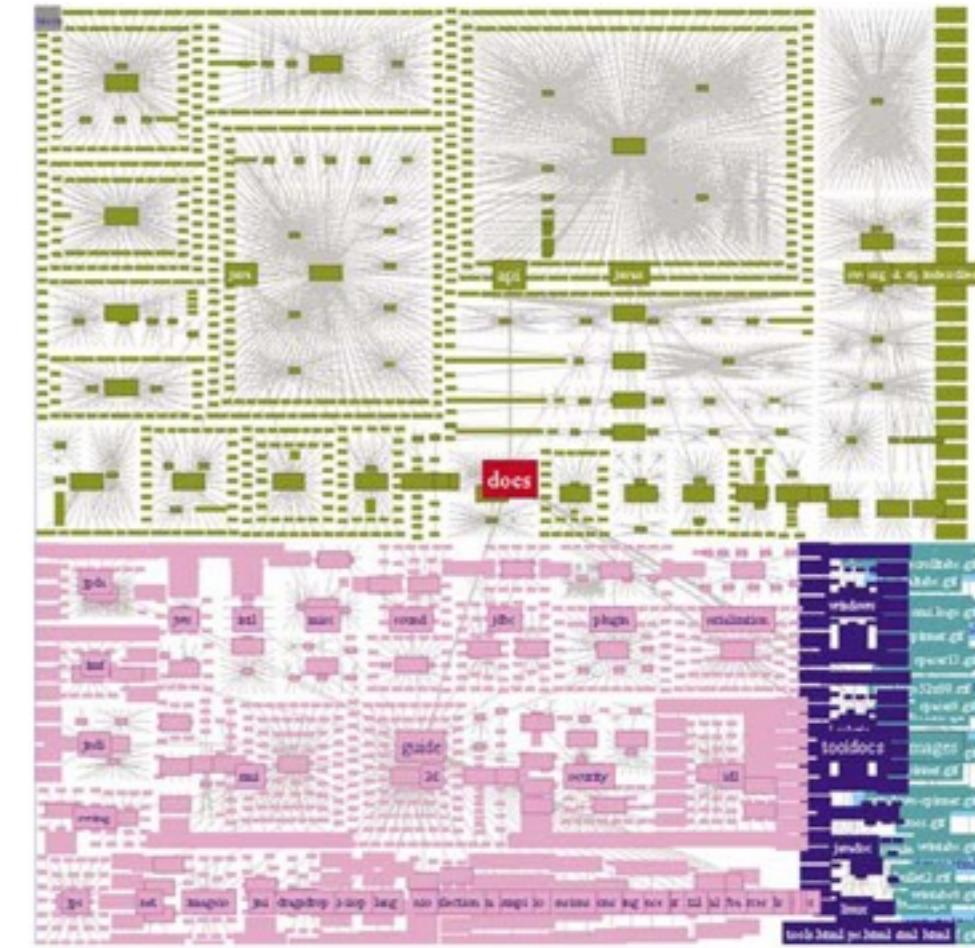
- Kay Wetzel (2003)
- Do not fill space completely,
- but...
  - Aspect ratio stays the same for all elements – easy comparison of sizes
  - Good visibility of nesting (though at the cost of unused space)
  - Rather beautiful layout!



Visualization of a file system with color mapping for creation data

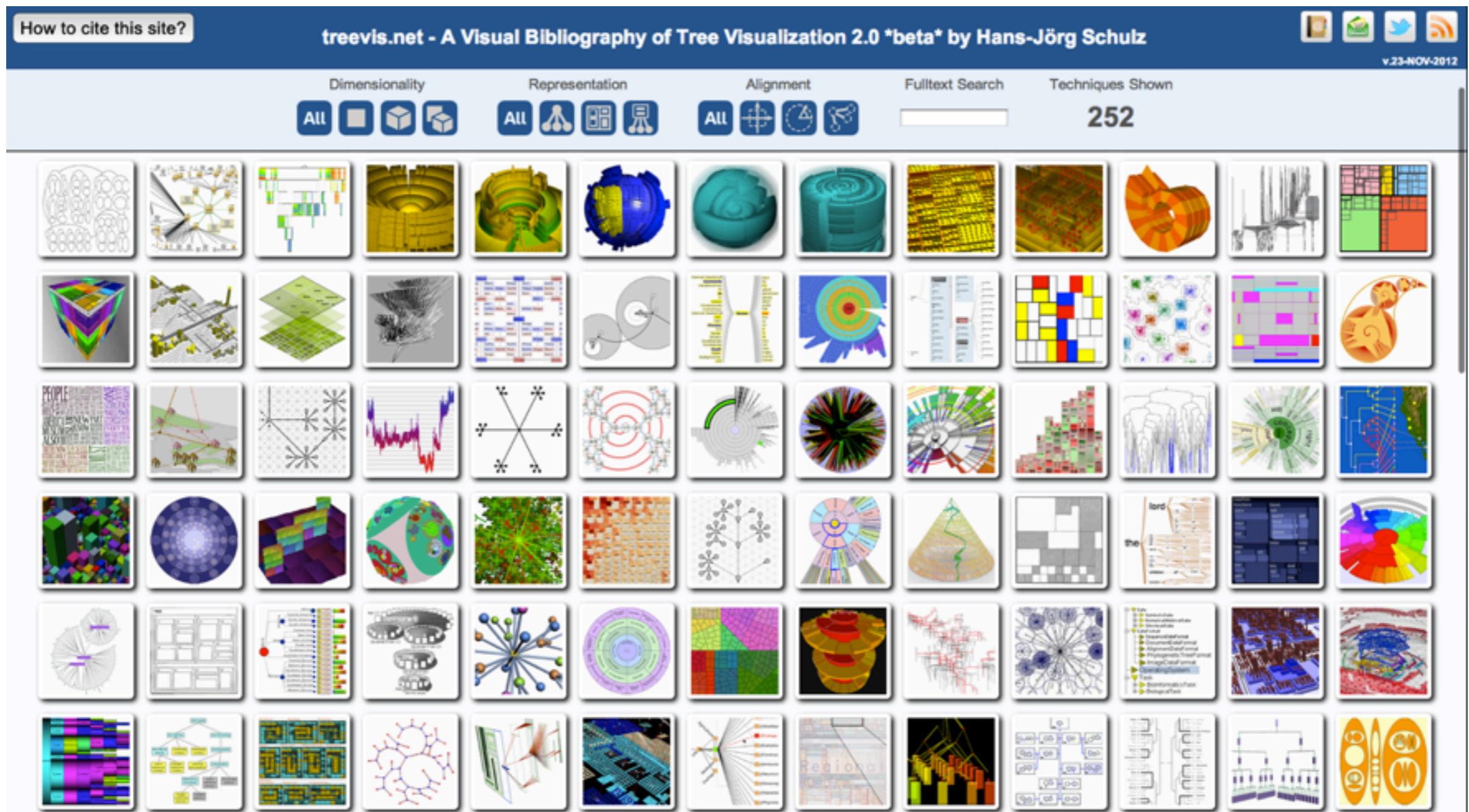
# Enclosure + Connection

- EncCON: Nguyen & Huang 2005
- Connection (node-link)
  - Gives immediate perception of data relationships and the tree structure
  - Not efficient regarding display space utilization: most pixels are wasted as background
- Enclosure (e.g. treemaps)
  - Space-filling approach allows the display large trees on a single glance
  - Focus on the leaf nodes but hardly conveys the tree structure
- Idea: combine enclosure and connection approach
- Child nodes are not embedded but placed around parent nodes using a circular, space-filling division method
- Focus+context navigation



Java SDK visualization – 9500 directories and files

# treevis.net: A Tree Visualization Reference



Schulz 2011

# Recommended Literature

- Benjamin B. Bederson & Ben Shneiderman ,  
"Ordered and Quantum Treemaps:  
Making Effective Use of 2D Space to Display  
Hierarchies", 2002.